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Trend Breaks and the Persistence of Closed-End Mutual Fund Discounts

Nazif Durmaz^{*}, Hyeongwoo Kim⁺, Hyejin Lee[‡] and Yanfei Sun[‡]

*Kean University, *Auburn University, *Tuskegee University, * Toronto Metropolitan University

AUWP 2023-03

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Trend Breaks and the Persistence of Closed-End Mutual Fund Discounts

Nazif Durmaz*, Hyeongwoo Kim[†], Hyejin Lee[‡], and Yanfei Sun[‡]

March 2023

Abstract

Closed-end fund (CEF) prices often exhibit large and persistent deviations from their associated net asset values (NAVs), which is puzzling since CEFs are repackaged financial assets and NAVs are publicly observable. We point out that such high persistence is mainly observed when linear models are employed, calling for nonlinear models to understand this so-called CEF discount puzzle. Applying the RALS-LM framework that allows for multiple endogenously identified trendbreaks for 31 CEF discount data, we show that CEF prices tend to fluctuate around time-varying time trends, which can be consistent with a regime switching model. We also demonstrate that utilizing non-normal errors through moment conditions enhances the efficiency at the margin. Nonlinearity with level shifts only fails to explain the observed persistence of CEF discounts.

Keywords: Closed-End Fund; CEF Discount Puzzle; Residual Augmented Least

Squares; Non-Normal Error; Trend Breaks

JEL Classification: C22; G12; G15

^{*} Global Business School, Kean University, 303-Q Hynes Hall, Union, NJ 07083, Tel: +1.908.737.4188, Email: ndurmaz@kean.edu.

[†] Department of Economics, Auburn University, 138 Miller Hall, Auburn, AL 36849. Tel: +1.334.844.2928. Email: gmmkim@gmail.com.

[‡] Department of Accounting, Economics & Finance, Tuskegee University, 1200 W Montgomery Rd, Tuskegee, AL 36088. Tel: +1.334.724.2018. Fax: +1.334.727.8604. Email: hlee@tuskegee.edu.

[#] Department of Finance, Toronto Metropolitan University, 350 Victoria Street, Toronto, ON, M5B 2K3, Canada. Tel: +1.416.979.500. Email: yanfei.sun@torontomu.ca.

1 Introduction

Fama (1970), in his influential survey article, suggests a market to be informationally efficient if the prices in the market fully reflect all available information that is relevant to their fundamental values. For example, stock prices should equal the present value of rationally expected future cash flows such as dividend payments. Although the efficient market hypothesis (EMH) provides an elegant and intuitive framework for asset pricing models, it is often a challenge to identify what fundamental variables drive and move the asset prices.

Campbell and Shiller (1988a, 1988b), Chen and Zhao (2009), and Chen, Da, and Zhao (2013) evaluated the empirical relevance of the present value model of stock prices. Specifically, Chen and Zhao (2009) and Chen *et al.* (2013) highlighted the important role of cash flow components of stock prices, separated from discount rate news that is more difficult to quantify. Roll (1988) and Morck, Yeung, and Yu (2000) decomposed stock returns into firm-specific news and market-wide news, and pointed out that stock prices often do not reflect individual firm-specific news relative to common market news.¹ More recently, Brogaard, Nguyen, Putnins, and Wu (2022) reported similar evidence that over 30% of stock return variations can be attributed to noise, while firm-specific information plays a much weaker role. On the other hand, Bai, Philippon, and Savov (2016) and Farboodi, Matray, Veldkamp, and Venkateswaran (2022) pointed out some, although limited, improvements in price informativeness in large and growth stocks.

Unlike most other financial assets, closed-end funds (CEFs) provide a straightforward and intriguing case in the price-fundamentals debate, because CEFs are in essence merely repackaged financial assets. One can identify the fundamental value of a CEF share price with its net asset value (NAV), which is the market value of the fund's portfolio divided by the number of shares. Since NAVs are publicly observable without delay, NAV allows for a direct and unambiguous inference regarding the intrinsic valuation of the fund. In the absence of substantial transaction costs, the CEF price should approximate its NAV, hence, deviations of CEF fund price from NAV should be short-lived.²

¹ For instance, weak protection of private property rights may make informed trading more difficult.

² Malkiel (1977, 1995), Thompson (1978) and Pontiff (1995) argue that if investors buy high discount shares and short sale low discount share, discount-based trading strategies may be profitable.

Yet it is well-known that CEFs normally trade at a discount, sometimes at a premium, to their NAV, and we often observe large and persistent deviations of CEF prices from their associated NAVs, presenting a challenge to conventional models of asset pricing.³ See, among others, Lee, Shleifer, and Thaler (1990, 1991), Ahmed, Koppl, Rosser, and White (1997), Gemmill and Thomas (2002), Hughen and Wohar (2006), and Berk and Stanton (2007).⁴

Many researchers put forward theoretical hypotheses for such puzzling phenomena, also known as the CEF Puzzle, such as investor sentiment (De Long, Shleifer, Summers, and Waldmann, 1990; Lee *et al.*, 1991; Chopra, Lee, Shleifer, and Thaler, 1993; Anderson, Beard, Kim, and Stern, 2013); arbitrage costs (Pontiff, 1996; Gemmill and Thomas, 2002); accumulated tax liability effects (Malkiel, 1995; Day, Li, and Xu, 2011); the structure of management fees and compensation (Ross, 2002; Berk and Stanton, 2007); and asset price bubbles (Jarrow and Protter, 2019).

This paper revisits the CEF Puzzle by employing an econometric model framework that allows multiple trend-breaks at unknown dates. We further utilize moment conditions to enhance the efficiency of estimations when the error term obeys a non-normal distribution. In what follows, we demonstrate that prolonged deviations of the fund price from its fundamentals are mainly observed when linear models are employed, even though these discounts often exhibit multiple long swings over time.

Long swings can be associated with a sequence of segmented time trends that are difficult to distinguish from a directionless drift of a random walk process. Since the seminal work of Nelson and Plosser (1982), many research works have been carried out with an assumption that macroeconomic time series contain a unit root. However, an array of researchers suggested that those series are better characterized by trend break models that allow structural breaks in time trend. See, among others, Perron (1989, 1997), Zivot and Andrews (1992), and Hsu and Kuan (2001).

³ Abraham, Elan, and Marcus (1993) find that bond CEFs exhibit premium trades whereas equity CEFs are usually trade at a discount. Anderson, Beard, Kim, and Stern (2016) also point out different short-run pricing behavior of stock and bond funds. CEF's initial public offerings (IPO) are usually at a premium and a study by Hanley, Lee, and Seguin (1996) explain this as brokers choice of marketing such funds to less informed traders.

⁴ Using hand-collected data, Bradley, Briav, Goldstein, and Jian (2010) introduce the possibility that activist arbitrages may reduce fund discounts. Open-ending the target CEF can force the managers to take corrective actions, because the price of the fund's shares will be forced to converge to its NAV.

We also note that such trend break models can be motivated by a regime switching model framework. In closely related work, Engel and Hamilton (1990) and Kaminsky (1993) employ Hamilton's (1989) framework for the dollar exchange rate that may be consistent with a sequence of segmented time trends. They show that such models can generate long swings that are often observed in the exchange rate data when the regimes have different signs and the transition probability matrix is close to be reducible.⁵ Although we do not employ regime switching models in this paper, our empirical model with trend breaks at endogenously chosen dates is consistent with such model specifications.

Recognizing that the CEF puzzle is often observed under the linear model framework, we investigate the role of nonlinear specifications to understand such highly persistent deviations of the CEF price from its fundamentals. For this purpose, we apply the residual augmented least squares (RALS) Lagrange multiplier (RALS-LM) unit root test framework for CEF discounts, which yields the efficiency gain by utilizing moment conditions when the error terms obey a non-normal distribution. Being motivated by persistent dynamics of CEF discounts that exhibit long swings, we allow endogenously identified multiple trend-breaks at unknown dates following the approach of Meng, Lee, and Payne (2017).

By implementing the nonlinear (trend breaks) RALS-LM test for 31 monthly frequency CEF discount data from January 1999 to April 2018, we obtained strong empirical evidence in favor of nonlinear stationarity around time-varying trends, which may help explain long-swing dynamics of CEF discounts. The RALS approach yields robust and sizable power gains by utilizing moment conditions embodied in non-normal errors. Allowing multiple trend breaks greatly enhances the efficiency of the test, while the efficiency gains from allowing level shifts only are negligible.

Organization of the paper is as follows. Section 2 introduces the data, then demonstrates the non-normal nature and high degree persistence of CEF discounts. Section 3 carefully describes the methodology used in the study. In Section 4, we report and discuss our major findings. Section 5 concludes.

⁵ For example, consider a data generating process (DGP) with two regimes. If the mean changes the sign across the regimes and if the diagonal elements of the transition matrix are close to one, such a DGP is likely to generate dynamics with long swings.

2 Stochastic Properties of Closed-End Fund Discounts

2.1 Data Descriptions and Summary Statistics

We obtained 31 daily frequency closed-end fund (CEF) prices and their net asset value (NAV) series from the Closed-End Fund Center (cefa.com) and Morningstar (morningstar.com). We transformed the daily frequency data to monthly data by taking the end of the month observations to reduce noise in the data. Observations span from January 1999 through April 2018. Discounts are constructed by taking the log difference of the price from NAV.⁶

Our data includes CEF discounts of 14 core stock funds, 6 corporate debt funds, and 11 general bond funds. Bond funds are selected from the Closed-End Fund Association's *General Bond* and *Corporate Debt BBB Rated Funds* categories, while stock funds are selected from the *Core Funds* category. We selected the funds with assets that exceed \$50 million (US) as of May 8, 2018.⁷ See Table 1 for the complete list of these mutual funds.

Table 1 around here

Figure 1 reports nine CEF discount graphs, three from each of the three categories. As mentioned before, long swings are observed in most discounts which imply the existence of multiple trend-breaks in the data generating process (DGP). For example, ADX exhibits roughly two swings, including the longer one that is bottoming around 2001, accompanied by a shorter swing in 2010's. MGF exhibits a downward time trend until around 2010 followed by an upward trend since then. See Appendix C for the complete set of figures with estimated time trends that will be explained in what follows.

Recall that such long swings can be associated with a sequence of segmented time trends that is difficult to distinguish from directionless drift of a random walk process. See Engel and Hamilton (1990) and Kaminsky (1993) for related discussion on the dollar exchange rate dynamics

⁶ That is, positive (negative) values imply the fund is traded at a discount (premium).

⁷ For more information on these Lipper classifications, see https://www.cefa.com.

using a regime switching model framework that can motivate our nonlinear trend break model in this paper.

Figure 1 around here

Table 2 presents summary statistics for these 31 CEF discounts. We first note that shares of most mutual funds are traded at a discount with exceptions of 7 out of 31 mutual funds, ranging from 14.99% average discount (ADX) to -17.23% average premium (CET). The skewness estimates don't exhibit any tendency, showing positively skewed distributions roughly as often as negatively skewed distributions. However, we observe leptokurtic distributions from all discounts that have kurtosis of 3 or higher, which implies a fat-tailed distribution. The Jarque-Bera test statistic (Jarque and Bera, 1980) implies strong evidence against the normal distribution based on the critical values from Deb and Sefton (1996).⁸

Table 2 around here

To help visualize the non-normal nature of the distribution of CEF discounts, Figure 2 presents kernel density estimates (solid lines) of 9 discounts along with their associated normal density function estimates (dashed lines), based on the estimated mean and standard deviation of the discounts. ^{9,10} Clearly, estimated kernel densities confirm the summary statistics in Table 2. They overall show fat-tail leptokurtic distributions. GAM and DUC even exhibit a bimodal distribution. That is, we observe strong evidence in favor of non-normal distributions in the CEF discounts, which provides solid justification for using the RALS-LM model specification in our paper.

Figure 2 around here

2.2 Persistence in CEF Discounts

⁸ The asymptotic critical values suggested by Jarque and Bera (1987) are known to have a size distortion problem.

⁹ We employed the Epanechnikov kernel to estimate the kernel density function.

¹⁰ Recall that the first and second moments are sufficient statistics for the normal distribution.

Let $dc_{i,t}$ be the discount of a mutual fund *i* as a percent (%) deviation of the share price $(P_{i,t})$ from its net asset value $(NAV_{i,t})$, that is, $dc_{i,t} = (\ln NAV_{i,t} - \ln P_{i,t}) \times 100$. Note that a positive (negative) value implies that the fund is traded at a discount (premium).

Consider the following linear Augmented Dickey-Fuller (ADF) regression model for the discount with an intercept.

$$dc_{i,t} = c_i + \alpha_i dc_{i,t-1} + \sum_{j=1}^k \beta_{i,j} \Delta dc_{i,t-j} + \varepsilon_{i,t}$$

It is well-known that the ordinary least squares (OLS) estimator of the persistence parameter α_i is biased.¹¹ Thus, we obtain the median unbiased estimate for the persistence parameter for each $dc_{i,t}$ via the grid bootstrap method (Hansen, 1999) as follows.

We implemented 10,000 nonparametric bootstrap simulations at each of 30 fine grid points, $\alpha_{i,j} \in \{\alpha_{i,1}, \alpha_{i,2}, ..., \alpha_{i,30}\}$, in the vicinity of $\hat{\alpha}_{i,OLS}$, $[\hat{\alpha}_{i,OLS} \pm 4se(\hat{\alpha}_{i,OLS})]$, to generate the p^{th} quantile function estimates with *T* observations, $\hat{q}_{T,p}^*(\alpha_{i,j}, \varphi(\alpha_{i,j}))$, where φ denotes nuisance parameters such as $\beta_{i,j}$. We obtain the median unbiased estimate $\hat{\alpha}_{i,MUE}$ by matching the grid-*t* statistics, $t = (\hat{\alpha}_{i,OLS} - \alpha_{i,j})/se(\hat{\alpha}_{i,OLS})$, with $\hat{q}_{T,0.5}^*(\alpha_{i,j}, \varphi(\alpha_{i,j}))$. The 95% confidence bands are similarly constructed utilizing $\hat{q}_{T,0.025}^*(\alpha_{i,j}, \varphi(\alpha_{i,j}))$ and $\hat{q}_{T,0.975}^*(\alpha_{i,j}, \varphi(\alpha_{i,j}))$.

In Table 3, we report $\hat{\alpha}_{i,MUE}$ and its associated 95% confidence band in addition to its implied half-life (HL) estimates.¹² $\hat{\alpha}_{i,MUE}$ point estimates are overall close to unity, ranging from 0.857 (INSI) to 1.001 (RVT), implying highly persistent dynamics of CEF discounts. Their associated half-life point estimates range from 4.49 months (INSI) to infinity (RVT). The median and the average half-life point estimates were 8.10 and 13.70 months, implying extremely long

¹¹ There exist both the median and the mean bias in the OLS estimator for the persistence parameter in the presence of deterministic terms. See Andrews (1993), Andrews and Chen (1994), and Hansen (1999) for median unbiased estimators and Kendall (1954), Shaman and Stine (1988), So and Shin (1999) for mean unbiased estimators. Mean unbiased estimates are quantitatively similar to the median unbiased estimates, although the confidence intervals tend to be finite more often.

¹² The half-life is defined as the time required for a deviation to half-way adjust to its long-run equilibrium. Half-lives are obtained by $\ln(0.5) / \ln(\hat{\alpha})$ assuming that deviations decay at a constant rate.

deviations of prices from their fundamentals. It should be noted that we obtain finite confidence bands only for 18 CEF discounts after correcting for median bias.¹³

Table 3 around here

3 The Econometric Model: Nonlinear RALS-LM Models

We investigate the observed high persistence of the closed-end fund (CEF) discounts by employing a RALS-LM model framework that allows not only level shifts (LS) but also trend breaks (TB) in the data generating process of the CEF discounts on endogenously identified structural break dates. Furthermore, this framework enhances the power by utilizing moment conditions based on nonnormal errors.

We employ the following two-step procedure. We first estimate break-related parameters using the maximum F test (max F) proposed by Lee, Strazicich, and Meng (2012). Given the estimated number and the location of breaks, the second step implements the RALS-LM unit root test. Dropping the subscript *i* for simplicity, consider the following data generating process (DGP) for dc_t .

$$dc_t = \boldsymbol{\delta}' \boldsymbol{d}_t + \varepsilon_t, \tag{1}$$

where ε_t denotes potentially serially correlated errors. For now, denote T_{Bi} the *known* location of the *i*th structural break (*i* = 1, 2, ..., *R*), while d_t , the vector of exogenous *deterministic* variables, is defined as follows.

(LS)
$$\boldsymbol{d}_t = [1, t, d_{1t}, ..., d_{Rt}]'$$
, or
(TB) $\boldsymbol{d}_t = [1, t, d_{1t}, ..., d_{Rt}, dt_{1t}, ..., dt_{Rt}]'$,

where

¹³ We also implement panel estimations for the persistence parameters using a fixed effect model by applying the grid bootstrap approach for the data after removing the fixed effect intercept. Results yielded a finite confidence band for the half-life, however, the implied half-life point estimate was over 137 months, confirming a substantial degree of persistence of the CEF discounts.

$$d_{it} = \begin{cases} 1, t \ge T_{Bi} + 1\\ 0, \text{ otherwise} \end{cases}$$
$$dt_{it} = \begin{cases} t - T_{Bi}, t \ge T_{Bi} + 1\\ 0, \text{ otherwise} \end{cases}$$

Based on the LM (score) procedure suggested by Schmidt and Phillips (1992), one can test the null hypothesis of the unit root using the *t*-statistics on $\phi = 0$ from the following regression.

$$\Delta dc_t = \boldsymbol{\delta}' \Delta \boldsymbol{d}_t + \boldsymbol{\phi} \widetilde{dc}_{t-1} + \sum_{j=1}^k \theta_j \, \Delta \widetilde{dc}_{t-j} + \boldsymbol{v}_t, \tag{2}$$

where $\widetilde{dc}_t = dc_t - \widetilde{\alpha} - \widetilde{\delta}' d_t$ is the LM detrended series (residuals) of dc_t . That is, $\widetilde{\delta}$ is the coefficient vector that is estimated by a separate regression, $\Delta dc_t = \delta' \Delta d_t + v_t$. $\tilde{\alpha}$ is the restricted MLE of α which is given by $\tilde{\alpha} = dc_1 - \tilde{\delta}' d_1$.¹⁴ Note also that (2) includes $\Delta d \tilde{c}_{t-j}, j = 1, ..., k$, to remove any existing serial correlations in the error term. The *t*-statistic for $\phi = 0$ from (2) is denoted by τ_{LM} .

As shown by Amsler and Lee (1995) and Lee and Strazicich (2003), the asymptotic distribution of τ_{LM} is invariant to the location and the magnitude of breaks when the model allows for breaks only in the level (LS). It should be noted, however, that the asymptotic distribution of τ_{LM} depends on the location of breaks in the model with trend breaks (TB). To control for such dependency on the nuisance parameter, Lee et al. (2012) suggest employing the transformed series \widetilde{dc}_t^* for TB model as follows by dividing \widetilde{dc}_t by the fraction of sub-samples in each regime: $\lambda_1^* =$ T_{B1}/T ; $\lambda_i^* = (T_{Bi} - T_{B(i-1)})/T$, i = 2, ..., R; $\lambda_{R+1}^* = (T - T_{BR})/T$.¹⁵

$$\widetilde{dc}_{t}^{*} = \begin{cases} \frac{\widetilde{dc}_{t}}{\lambda_{1}^{*}} &, \text{ for } t \leq T_{B1} \\ \frac{\widetilde{dc}_{t}}{\lambda_{2}^{*}} &, \text{ for } T_{B1} < t \leq T_{B2} \\ \vdots \\ \frac{\widetilde{dc}_{t}}{\lambda_{R+1}^{*}} &, \text{ for } T_{BR} < t \leq T \end{cases}$$

$$(3)$$

¹⁴ $d_t = [1, t]'$ that allows no break gives the LM statistic of Schmidt and Phillips (1992). ¹⁵ See Proposition 1 in Lee *et al.* (2012).

Replacing \widetilde{dc}_{t-1} in the testing regression (2) with \widetilde{dc}_{t-1}^* , we obtain the following.

$$\Delta dc_t = \boldsymbol{\delta}' \Delta \boldsymbol{d}_t + \boldsymbol{\phi} \widetilde{dc}_{t-1}^* + \sum_{j=1}^k \theta_j \, \Delta \widetilde{dc}_{t-j} + \boldsymbol{e}_t \tag{4}$$

Let τ_{LM}^* be the *t*-statistic for $\phi = 0$ from (4). As Lee *et al.* (2012) indicated, under this transformation, the asymptotic distribution of τ_{LM}^* depends on the number of trend-breaks instead of the location of breaks. That is, one can use the critical values of τ_{LM}^* that correspond to the number of breaks instead of simulated critical values at the estimated optimal break points.¹⁶

We now turn back to the first stage of our testing procedure to endogenously identify the break parameters. Following Lee *et al.* (2012), we employ an *F*-statistic approach to identify the location of breaks along with the optimal number of lags as follows.

$$F = \frac{(SSR_0 - SSR_1(\lambda))/m}{SSR_1(\lambda)/(T-q)},$$
(5)

where *m* is the number of restrictions (i.e., number of level shifts in the LS model and number of trend-breaks in the TB model) and *q* denotes the number of regressors in (4). SSR_1 is the sum of the squared residuals from (4), while SSR_0 is the sum of the squared residuals from the LM unit root test without break (Schmidt and Phillips, 1992) with $d_t = [1, t]'$ in (2).

More specifically, we set a maximum number of breaks \overline{R} and determine the number of lag augmentations using the general-to-specific procedure. Via a grid search, we identify the location of breaks where the *F*-statistic is maximized, simultaneously considering the estimated optimal lags and the corresponding number of breaks. Next, one can determine the number of structural changes by examining the significance of dummy coefficients with the usual *t*-test. If one or more number of the break dummies are insignificant based on the standard *t*-test, one can move to the first step with the break number of $\overline{R} - 1$. Once the number and the location of breaks are determined, one can implement the unit root test based on equation (4).

Finally, we employ the RALS (Im and Schmidt, 2008) approach-based procedure of Meng *et al.* (2017) which extended the RALS unit root test of Meng, Im, Lee, and Tieslau (2014) by

¹⁶ The critical values of the transformed LM tests with trend shifts are presented in Im, Lee, and Tieslau (2010) for R = 1, 2, 3.

allowing for structural breaks. Meng *et al.* (2017) showed that the power of the RALS unit root procedure is superior to that of the two step-based LM tests in (4) when the error term follows a non-normal distribution. The RALS unit root test is implemented via the following two-step procedure.

First, we obtain the least square residual \hat{e}_t by estimating equation (4) and construct \hat{w}_t given by,

$$\widehat{\boldsymbol{w}}_t = \boldsymbol{h}(\widehat{\boldsymbol{e}}_t) - \frac{1}{T} \sum_{s=1}^T \boldsymbol{h}(\widehat{\boldsymbol{e}}_s) - \widehat{\boldsymbol{e}}_t \cdot \frac{1}{T} \sum_{s=1}^T \boldsymbol{h}'(\widehat{\boldsymbol{e}}_s),$$
(6)

where $h(\cdot)$ is a $J \times 1$ known differentiable function. And For the RALS(2&3) test, define $h(\hat{e}_t)$ as a vector of the function of the second and the third moments, $h(\hat{e}_t) = [\hat{e}_t^2, \hat{e}_t^3]'$, which results in the following.

$$\widehat{\boldsymbol{w}}_t = \begin{bmatrix} \hat{e}_t^2 - \hat{m}_2 \\ \hat{e}_t^3 - \hat{m}_3 - 3\hat{m}_2\hat{e}_t \end{bmatrix},\tag{7}$$

where \hat{m}_j denotes the *j*th sample moment of its corresponding population moment, $m_j = E(e_t^j)$. The first term in (7) exploits the condition of *no heteroscedasticity* while the second term improves the efficiency unless the *redundancy condition* is met. It turns out that augmenting equation (4) with \hat{w}_t in (7) increases efficiency and results in higher power in the RALS-LM tests relative to the LM tests in (4) unless the error term e_t follows a normal distribution.¹⁷

The RALS(t_v) test is based on an assumption that the error term obeys a *t*-distribution with v degrees of freedom. For this, we choose a scalar differentiable function $h(\hat{e}_t) = \frac{(v+1)\hat{e}_t}{v+\hat{e}_t^2}$ that yields the following.¹⁸

$$\widehat{w}_{t} = \frac{(\nu+1)\hat{e}_{t}}{\nu+\hat{e}_{t}^{2}} - \frac{1}{T}\sum_{s=1}^{T}\frac{(\nu+1)\hat{e}_{s}}{\nu+\hat{e}_{s}^{2}} - \hat{e}_{t} \cdot \frac{1}{T}\sum_{s=1}^{T}\frac{(\nu+1)(\nu-\hat{e}_{s}^{2})}{(\nu+\hat{e}_{s}^{2})^{2}}$$
(8)

¹⁷ It is known that the normal distribution of the error term satisfies the redundancy condition $m_{j+1} = j\sigma^2 m_{j-1}, j = 2, 3$, where m_j is the j^{th} central moment. See Breusch, Qian, Schmidt, and Wyhowski (1999) for details. Specifically, the normal distribution is the only distribution that satisfies $m_4 = 3\sigma^4$.

¹⁸ Meng et al. (2014) provide a robustness check with alternative degrees of freedom.

We employ the *t*-distribution with *v* degrees of freedom to mimic fat-tailed distributions that are often observed in financial market data such as the mutual fund discount data used in this paper, as shown earlier. Meng *et al.* (2014) demonstrated that the additional term \hat{w}_t results in efficiency gains under fat-tailed types of distributions.

Unlike the RALS(2&3) approach, the efficiency gain of using the RALS(t_v) procedure does not require any redundancy condition. Note that $h(\hat{e}_t) = \frac{(v+1)\hat{e}_t}{v+\hat{e}_t^2}$ is derived from the score vector of the MLE with an assumption that observations are randomly drawn from the generalized *t*distribution (see Appendix A for its derivation). That is, we employ such score function as the moment condition to enhance the efficiency of the RALS-LM test in the spirit of the GMM estimator.

Finally, the RALS-LM test statistic with trend-breaks is obtained from the following regression by augmenting equation (4) with the constructed variable \hat{w}_t in (7) or (8).

$$\Delta dc_t = \boldsymbol{\delta}' \Delta \boldsymbol{d}_t + \boldsymbol{\phi} \widetilde{dc}_{t-1}^* + \boldsymbol{\gamma}' \widehat{\boldsymbol{w}}_t + \sum_{j=1}^k \theta_j \, \Delta \widetilde{dc}_{t-j} + u_t.$$
(9)

The null hypothesis of the unit root is tested using the *t*-statistics on $\phi = 0$ from (9). When the distribution of the error term follows a non-normal distribution, the added term \hat{w}_t works as the stationary covariate, similar as in Hansen (1995), and the error variance in the RALS-LM tests from (9) becomes smaller than that in equation (4). Accordingly, the RALS tests become more efficient and achieve higher power.

We denote the test statistic from the RALS-LM test with trend-shifts as $\tau_{RALS-LM}^*$. As shown by Meng *et al.* (2017), the asymptotic distribution of $\tau_{RALS-LM}^*$ depends on ρ^2 which can be estimated as,

$$\hat{\rho}^2 = \frac{\hat{\sigma}_R^2}{\hat{\sigma}^2},\tag{10}$$

where $\hat{\sigma}_R^2$ and $\hat{\sigma}^2$ are the estimated variances of the regression in (9) and (4), respectively. With the transformation, the asymptotic distribution of the RALS-LM test statistic with trend-breaks no

longer depends on the break location parameters. The RALS-LM tests with trend-breaks can be implemented using the appropriate critical values reported in Table 1 of Meng *et al.* (2017).¹⁹

4 The Empirics

4.1 **Power Gains from Utilizing Non-Normal Errors: Linear RALS Unit Root Test**

We first report benchmark linear unit root test results with no structural break in order to investigate the power gains from non-normal errors only. For this purpose, we employ the following RALS regression equation with a time-invariant intercept as in Meng *et al.* (2014).

$$\Delta dc_t = \alpha + \phi dc_{t-1} + \gamma' \widehat{w}_t + \sum_{i=1}^k \theta_i \Delta dc_{t-i} + u_t$$
(11)

which is equivalent to the Augmented Dickey-Fuller (ADF) regression equation in the absence of \hat{w}_t term ($\gamma = 0$). Note that this benchmark procedure requires neither any transformations nor LM detrending for dc_t .

We chose the optimal number of lags based on the general-to-specific rule with a maximum of 10 lags. The asymptotic critical values for the RALS tests depend on $\hat{\rho}^2 = \hat{\sigma}_{RALS}^2 / \hat{\sigma}_{ADF}^2$ from (11), which is similarly defined as the ratio of the error variance estimates in (10). The critical values were obtained from Hansen (1995). Test results are reported in Table 4.

$$\tau_{RALS-LM} = \rho \tau_{LM} + \sqrt{1 - \rho^2} Z \tag{FN.1}$$

¹⁹ Due to the invariance property of the level shifts (LS) model, indicated in Amsler and Lee (1995) and Lee and Starazicich (2003), the critical value of the LM unit root tests with the LS model is the same as that of Schmidt and Phillips (1992). Therefore, as Lemma 1 of Meng *et al.* (2014) shows, the limiting distribution of the RALS-LM tests with level shifts is as follows.

where $\tau_{RALS-LM}$ is the *t*-statistic for $\phi = 0$ from the RALS regression (9), τ_{LM} is the *t*-statistic for $\phi = 0$ in (2) while assuming $d_t = [1, t]'$ (Schmidt and Phillips, 1992), and ρ denotes the weighting parameter. Note that the invariance property allows the RALS-LM unit root tests with level shifts to be implemented without the transformation procedure in (3). In addition to this, the limiting distribution of (FN.1) is the same as that of the RALS-LM tests without breaks. This implies that the same set of critical values can be used for the RALS-LM unit root test for both the no-break and level shift models regardless of the number of shifts. Therefore, to implement both tests, one can obtain the estimated error variance of the RALS tests ($\hat{\sigma}_R^2$) from (9) without a transformation and $\hat{\sigma}^2$ from equation (2) while assuming $d_t = [1, t]'$ and $d_t = [1, t, D_{1t}, ..., D_{Rt}]'$ for the no-break model and for the level shifts model, respectively, and make a decision using the same set of critical values reported in Table 11.1 of Meng *et al.* (2014).

The ADF test rejects the null hypothesis of nonstationarity for 12 out of 31 mutual fund discounts at the 5% significance level (38.7%), while 4 more cases are rejected at the 10% level. The RALS(2&3) test rejects the null of nonstationarity for 18 out of 31 cases at the 5% significance level (61.3%). The RALS(t₅) test rejects the null for 16 and 18 mutual fund discounts at the 5% and the 10% significant levels, respectively, for all degrees of freedom we considered. See Table B1 for alternative degrees of freedom (ν) in Appendix B.

These findings imply considerable power gains by utilizing distribution information of non-normal errors in the mutual fund discounts. The RALS test rejects the null hypothesis for up to 6 more cases at the 5% significance level in comparison with the ADF test results, although both tests reject roughly the same number of cases at the 10% level. Put it differently, adding a distributional assumption seems to strengthen the power at the margin. In what follows, we investigate the possibility of adding further power gains by allowing structural breaks at unknown dates.

Table 4 around here

4.2 **Power Gains from Time-Dependent Nonlinearity**

This section reports the RALS-LM unit root test results allowing both the level shifts and the trendbreaks at unknown dates via the procedures explained in Section 3.

Tables B2 and B3 in Appendix B provide the LM and RALS-LM unit root test results allowing level shifts but not trend-breaks. We note that allowing level-shifts only fails to generate any power gains even when additional distributional assumptions are added via RALS procedures. As can be seen in Table B2, the LM test with one identified structural break in level rejects the null of nonstationarity only for 10 mutual fund discounts at the 10% significance level. The RALS-LM(2&3) and RALS-LM(t_v) performed similarly. Allowing for two level-shifts doesn't change the performance of the test, rejecting up to 11 discounts. See Table B3.

These findings imply a possible misspecification problem in a model with time-varying intercepts. Given such findings, we switch our attention to the RALS-LM unit root test that allows trend-breaks. As seen in Figure 1, there exists strong visual evidence of time-varying time trends in our mutual fund discount data. To statistically evaluate such a possibility, we implement the

RALS-LM test based on equations (7), (8), and (9) that allows up to two trend breaks at unknown dates. We report substantial empirical evidence in favor of nonlinear stationarity in Tables 5, 6, and 7.

Table 5 reports results from benchmark models with $d_t = [1, t]'$ but without allowing any structural break in time trend. The LM test by Schmidt and Phillips (1992) rejects the null of nonstationarity for 10 discounts at the 10% significance level, while adding distributional assumptions via the RALS principle improves the power by rejecting additional 2 or 4 more cases.

According to Figure 1, the visual inspections in favor of nonlinear stationarity and the results in Table 5 seem to provide strong evidence in favor of the initial findings of Perron (1989), who noted that unit root tests lose power if existing breaks are ignored. Lee and Hur (2021) indicate that the power of the test decreases when the RALS tests do not take into account the on-going structural breaks in the data. In this regard, we believe that extending the RALS unit root tests to explicitly consider ongoing structural breaks in the testing regression would be a meaningful contribution in examining the CEF discount data.

Table 5 around here

Indeed, allowing one deterministic trend break yields substantial power gains as can be seen in Table 6. The LM test rejects the null hypothesis for 16 mutual fund discounts at the 10% significance level. The RALS-LM tests reject the null for up to 19 out of 31 discounts at the 10% level. The RALS-LM(t₅) test rejects the null for 20 discounts at the 10% level. Comparing these findings with the ones in Tables 5, B2, and B3, we see that allowing nonlinearity with a trend-break yields significant improvement with or without adding information on non-normal errors.

We further implement our investigation with two trend-breaks. Results are reported in Table 7. Note that the LM test rejects the null for 13 additional discounts, that is a total of 29 out of 31 discounts. The RALS-LM tests yield similar evidence of nonlinear stationarity by rejecting the null for almost all cases no matter what RALS methodologies are used.

It should be noted that this by no means is the result of allowing additional flexibility in modelling the time trend. As one can see in Tables B2 and B3, we obtained roughly the same weak evidence of nonlinear stationarity even when two level-shifts were allowed. These findings imply an important role of allowing time-varying time trends in the mutual fund discount dynamics over

time, which is also consistent with regime switching models that generate long swings in the financial data.

Tables 6 and 7 around here

5 Concluding Remarks

The net asset value (NAV) of a closed-end fund (CEF) allows for direct information on the intrinsic value of the fund, providing a straightforward case as to the identification of the underlying fundamental forces that drive and move the asset prices. Therefore, when informed trading is feasible and if the transaction costs are not substantial, deviations of CEF prices from their associated NAVs should be short-lived. However, we often observe substantial and highly persistent deviations, which is hard to reconcile with regards to the reasonings based on the efficient market hypothesis (EMH). This paper presents an alternative empirical framework to understand this well-known CEF Puzzle.

We employ a nonlinear RALS-LM framework for 31 monthly frequency CEF discount data from January 1999 to April 2018, allowing multiple trend-breaks at endogenously identified dates. We show that introducing nonlinearity via level shifts is not helpful to understand highly persistent dynamics of the CEF discount, while trend-breaks are the key to explain persistent deviations of CEF prices from their fundamentals. That is, CEF prices seem to fluctuate around time-varying trends, generating persistent long-swing dynamics of discounts, which can be consistent with regime-switching models with a near reducible transition matrix. Also, our empirical findings show that efficiency gains from utilizing moment conditions based on non-normal errors also arise on the margin.

The findings presented in this paper provide practically useful information for investment strategies, because deviations of CEF prices from their NAVs do not necessarily imply any immediate change of course. That is, price reversals are not likely to occur at short investment horizons. As is shown in our paper, persistent deviations of CEF prices can be associated with long-swings, providing empirical support in favor of momentum investment strategies because identified trends are likely to continue.

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Figure 1. Mutual Fund Discounts

Note: We obtained the data from the Closed-End Fund Center (cefa.com) and Morningstar (morningstar.com). We transform the daily frequency data to monthly frequency data by taking end of the period values. The discount is defined as a percent (%) deviation of the fund price from its net asset value. The sample period is from January 1999 to April 2018. See the Appendix for all discount graphs.



Figure 2. Kernel Density Estimates of Mutual Fund Discounts

Note: We estimated the Kernel density function of mutual fund discounts assuming an Epanechnikov kernel. Dashed lines are the normal density function estimates utilizing the first and second moments of each discount. Kernel density estimates of all discounts are available upon request.

Categories	Fund Name	Total Net Assets (\$ Mil)
Core Funds	Adams Diversified Equity (ADX)	1,771.6
	Central Securities Corp (CET)	821.4
	Cornerstone Strat Value (CLM)	563.3
	Cornerstone Total Return (CRF)	277.2
	Gabelli Equity Trust (GAB)	2,044.7
	General Amer Investors (GAM)	1,037.1
	Eagle Capital Growth (GRF)	33.3
	Royce Micro-Cap Trust (RMT)	412.1
	Royce Value Trust (RVT)	1,446.2
	Source Capital (SOR)	382.6
	Special Opportunities Fd (SPE)	142.5
	Tri-Continental Corp (TY)	1,609.7
	Sprott Focus Trust (FUND)	220.3
	Liberty All-Star Equity (USA)	1,302.0
Corp Debt BBB	Morg Stan Income Sec (ICB)	168.3
	MFS Govt Markets Inc Tr (MGF)	157.9
	MFS Intermediate Income (MIN)	494.0
	Insight Select Income (INSI)	216.8
	Western Asset Income (PAI)	139.6
	Invesco Bond Fund (VBF)	219.9
General Bond	Duff & Phelps Util&Corp (DUC)	261.5
	J Hancock Investors (JHI)	241.0
	Deutsche Mlti-Mkt Inc Tr (KMM)	203.1
	Deutsche Strat Inc Tr (KST)	55.2
	Barings Corporate Inv (MCI)	303.5
	MFS Charter Income Trust (MCR)	428.8
	MFS Multimkt Inc Tr (MMT)	432.9
	Barings Part Investors (MPV)	145.5
	PCM Fund (PCM)	118.4
	Putnam Mstr Intmdt Incom (PIM)	271.3
	Putnam Premier Income (PPT)	602.1

Table 1. Closed-End Mutual Fund Information

Note: We obtained the data from the Closed-End Fund Center (cefa.com) and Morningstar (morningstar.com). Total net asset values shown in million dollars are as of May 8, 2018.

Categories	Fund	Mean	SD	Skew	Kurt	JB
Core Funds	ADX	14.99	2.36	-0.58	6.12	106.62
	CET	-17.23	3.73	0.33	5.85	82.32
	CLM	14.65	20.11	-1.70	13.86	1,245.02
	CRF	8.63	40.39	-1.72	21.99	3,583.00
	FUND	9.51	7.51	-0.46	5.42	64.34
	GAB	-2.08	7.58	-0.01	4.56	23.44
	GAM	12.93	4.66	0.26	11.45	689.64
	GRF	-7.27	10.97	0.43	5.90	88.14
	RMT	10.35	7.18	0.18	4.03	11.48
	RVT	8.50	8.16	0.09	4.01	10.16
	SOR	2.73	10.77	-0.14	4.87	34.28
	SPE	-11.53	3.53	0.08	4.62	25.55
	TY	14.84	3.34	0.28	8.47	291.09
	USA	8.77	8.81	0.42	5.97	91.47
Corp Debt BBB	ICB	7.09	4.07	-0.32	6.16	99.92
	INSI	8.96	3.72	0.94	7.36	217.11
	MGF	6.70	5.26	0.06	10.24	505.06
	MIN	7.14	4.88	0.63	6.23	115.87
	PAI	5.85	5.12	-0.31	4.71	31.79
	VBF	7.04	5.00	-0.11	4.28	16.19
General Bond	DUC	0.99	6.31	-0.29	4.82	35.11
	JHI	3.47	8.21	-0.04	4.12	12.16
	KMM	2.90	8.11	0.33	4.59	28.35
	KST	2.07	9.80	-0.10	7.79	220.92
	MCI	-9.94	10.95	0.47	4.19	22.19
	MCR	9.49	3.58	0.05	4.95	36.55
	MMT	9.78	3.68	0.27	4.10	14.44
	MPV	-8.02	10.54	-0.39	6.89	151.55
	PCM	-5.23	7.16	1.17	6.69	183.56
	PIM	7.44	5.31	0.17	6.20	99.83
	PPT	7.69	5.36	-0.04	8.77	320.59

Table 2. Summary Statistics

Note: The discount is defined as a percent (%) deviation of the fund price from its net asset value. The sample period is from January 1999 to April 2018. We transform the daily frequency data to monthly frequency data by taking end of the period values. JB refers to the normality test statistics by Jarque and Bera (1980, 1987), of which the null hypothesis is that the discount is normally distributed. The null hypothesis was rejected for all fund discounts at the 5% significance level. The critical values were taken from Deb and Sefton (1996) to overcome a size distortion problem using an asymptotic chi-square distribution with the two degrees of freedom.

Categories	Fund	α_{MUE}	LB	UB	HL	HLB	HUB
Core Funds	ADX	0.910	0.835	1.001	7.344	3.840	∞
	CET	0.914	0.833	1.013	7.704	3.792	∞
	CLM	0.947	0.899	1.006	12.732	6.516	∞
	CRF	0.979	0.946	1.012	32.664	12.492	∞
	GAB	0.916	0.857	0.980	7.896	4.488	34.308
	GAM	0.980	0.915	1.028	34.308	7.800	∞
	GRF	0.955	0.886	1.023	15.060	5.724	∞
	RMT	0.971	0.918	1.019	23.556	8.100	∞
	RVT	1.001	0.950	1.025	∞	13.512	∞
	SOR	0.987	0.944	1.019	52.968	12.024	∞
	SPE	0.869	0.789	0.954	4.932	2.928	14.724
	TY	0.901	0.832	0.981	6.648	3.768	36.132
	FUND	0.981	0.920	1.026	36.132	8.316	∞
	USA	0.975	0.928	1.017	27.372	9.276	∞
Corp Debt BBB	ICB	0.892	0.817	0.976	6.060	3.432	28.536
	MGF	0.940	0.886	1.008	11.208	5.724	∞
	MIN	0.959	0.906	1.016	16.560	7.020	∞
	INSI	0.857	0.775	0.943	4.488	2.724	11.808
	PAI	0.859	0.780	0.941	4.560	2.784	11.400
	VBF	0.917	0.859	0.982	8.004	4.560	38.160
General Bond	DUC	0.925	0.861	1.006	8.892	4.632	∞
	JHI	0.968	0.917	1.016	21.312	8.004	∞
	KMM	0.951	0.891	1.015	13.800	6.000	∞
	KST	0.935	0.885	0.995	10.308	5.676	138.288
	MCI	0.918	0.844	1.010	8.100	4.092	∞
	MCR	0.900	0.833	0.974	6.576	3.792	26.316
	MMT	0.900	0.829	0.982	6.576	3.696	38.160
	MPV	0.890	0.812	0.976	5.952	3.324	28.536
	PCM	0.916	0.848	0.999	7.896	4.200	692.796
	PIM	0.921	0.857	1.004	8.424	4.488	00
	PPT	0.900	0.830	0.980	6.576	3.720	34.308

Table 3. Persistence Properties of Closed-End Mutual Fund Discounts

Note: (a) α_{MUE} denotes the persistence parameter estimate from AR(*p*) that is corrected for median bias following Hansen's (1999) grid bootstrap approach. We implemented 10,000 bootstrap iterations at 30 fine grid points in the viscinity of the OLS estimate, $[\hat{\alpha}_{OLS} - 4 \times se, \hat{\alpha}_{OLS} + 4 \times se]$. The 95% confidence band [LB,UB] is similarly constructed. HL denotes the implied half-life estimate in month, and its 95% confidence band is [HLB,HUB]. The median and the average HL estimates were 8.10 and 13.70 months, respectively.

Categories	Fund	$ au_{ADF}$	$ au_{RALS(2\&3)}$	$\hat{ ho}_{(2\&3)}^2$	$\tau_{RALS(t_5)}$	$\hat{ ho}_{(t_5)}^2$	ƙ
Core Funds	ADX	-2.719 [*]	-3.475‡	0.861	-3.470 [‡]	0.778	8
	CET	-2.470	-1.854	0.786	-2.080	0.630	5
	CLM	-1.843	-0.629	0.701	-1.768	0.854	10
	CRF	-2.248	-1.115	0.642	-1.888	0.728	0
	FUND	-1.892	-2.259	0.854	-2.596*	0.750	2
	GAB	-3.419†	-2.825†	0.858	-3.316 [†]	0.830	0
	GAM	-2.045	-3.845 [‡]	0.623	-3.286 [‡]	0.475	9
	GRF	-1.510	-2.747†	0.786	-1.760	0.856	10
	RMT	-1.675	-1.609	0.898	-1.744	0.823	10
	RVT	-1.721	-1.854	0.912	-1.808	0.814	7
	SOR	-1.335	-1.753	0.812	-1.509	0.616	3
	SPE	-3.769 [‡]	-2.995†	0.844	-3.973 [‡]	0.657	1
	TY	-3.588 [‡]	-3.153†	0.608	-3.746‡	0.397	6
	USA	-2.104	-1.985	0.742	-1.895	0.510	1
Corp Debt BBB	ICB	-3.308 [†]	-3.951‡	0.794	-4.383 [‡]	0.650	7
	INSI	-3.603 [‡]	-3.836‡	0.840	-3.821‡	0.763	5
	MGF	-2.305	-3.159†	0.710	-3.048†	0.623	8
	MIN	-2.290	-0.981	0.843	-0.804	0.799	5
	PAI	-3.377 [†]	-2.943†	0.849	-3.305 [†]	0.823	8
	VBF	-3.418 [†]	-3.387‡	0.891	-3.111 [†]	0.842	3
General Bond	DUC	-2.990†	-1.894	0.854	-0.788	0.754	1
	JHI	-2.254	-2.233	0.925	-2.134	0.875	1
	KMM	-2.760^{*}	-3.257^{\dagger}	0.871	-3.248‡	0.676	7
	KST	-2.530	-2.343	0.727	-2.934 [†]	0.626	10
	MCI	-2.899†	-3.535‡	0.886	-2.827^{\dagger}	0.959	2
	MCR	-3.528 [‡]	-3.253†	0.876	-2.700^{*}	0.826	1
	MMT	-3.362 [†]	-3.712 [‡]	0.906	-3.445‡	0.843	1
	MPV	-3.352 [†]	-4.090‡	0.782	-2.804^{\dagger}	0.750	8
	PCM	-2.535	-2.855†	0.665	-1.510	0.915	4
	PIM	-2.843*	-2.847^{\dagger}	0.760	-3.245 [‡]	0.586	8
	PPT	-2.719 [*]	-2.118	0.816	-1.487	0.674	10

Table 4. ADF and RALS Unit Root Test Results

Note: (a) τ_{ADF} , $\tau_{RALS(2\&3)}$, and $\tau_{RALS(t_5)}$ are the test statistics for the ADF, RALS(2&3), and RALS(t_5) tests, respectively. (b) $\hat{\rho}^2_{(2\&3)}$ and $\hat{\rho}^2_{(t_5)}$ indicate the ratio of the estimated error variances for RALS(2&3) and RALS(t_5) tests, respectively. (c) We chose the optimal number of lags (\hat{k}) based on the general-to-specific rule with a maximum 10 lags. (d) *, † and ‡ denote a rejection of the null hypothesis of nonstationarity at the 10%, 5% and 1% significance level, respectively. (e) The critical values of RALS tests are dependent on $\hat{\rho}^2$ and were obtained from Hansen (1995).

Categories	Fund	$ au_{LM}$	$ au_{RALS-LM(2\&3)}$	$\hat{ ho}_{(2\&3)}^2$	$\tau_{RALS-LM(t_5)}$	$\hat{ ho}_{(t_5)}^2$
Core Funds	ADX	-1.627	-2.481	0.870	-2.127	0.777
	CET	-2.714	-1.953	0.795	-2.217	0.635
	CLM	-1.492	-0.207	0.711	-1.270	0.880
	CRF	-2.157	-1.021	0.644	-1.742	0.577
	FUND	-1.535	-1.642	0.869	-1.673	0.767
	GAB	-3.563†	-2.987†	0.867	-3.523†	0.832
	GAM	-2.569	-4.349‡	0.621	-4.027‡	0.476
	GRF	-1.846	-3.054†	0.793	-2.247	0.853
	RMT	-1.219	-0.975	0.912	-0.971	0.831
	RVT	-1.333	-1.387	0.923	-1.303	0.820
	SOR	-1.839	-2.160	0.825	-2.045	0.618
	SPE	-3.726‡	-5.367‡	0.286	-6.328‡	0.230
	TY	-2.728	-1.987	0.594	-2.711†	0.361
	USA	-1.959	-1.787	0.748	-1.632	0.513
Corp Debt BBB	ICB	-3.221†	-3.873‡	0.802	-4.280‡	0.653
	INSI	-3.719‡	-3.931‡	0.850	-4.028‡	0.766
	MGF	-2.423	-3.485‡	0.706	-3.529‡	0.617
	MIN	-2.287	-1.004	0.852	-0.780	0.807
	PAI	-2.470	-2.074	0.848	-2.570	0.806
	VBF	-3.255†	-3.264†	0.896	-2.949*	0.844
General Bond	DUC	-3.592†	-2.793*	0.879	-2.416	0.825
	JHI	-2.115	-2.059	0.933	-2.029	0.873
	KMM	-2.438	-2.748*	0.883	-2.534	0.697
	KST	-2.468	-2.196	0.737	-2.400	0.699
	MCI	-2.865*	-3.497†	0.893	-2.800*	0.964
	MCR	-2.864*	-2.635	0.867	-2.212	0.795
	MMT	-3.229†	-3.443†	0.917	-3.269†	0.843
	MPV	-3.305†	-4.039‡	0.788	-2.843*	0.746
	PCM	-2.063	-2.325	0.677	-1.119	0.890
	PIM	-2.603	-2.784*	0.760	-3.126†	0.577
	PPT	-2.218	-1.789	0.812	-1.530	0.633

Table 5. LM and RALS-LM Test Results with No Trend Break

Note: (a) τ_{LM} , $\tau_{RALS-LM(2\&3)}$, $\tau_{RALS-LM(t_5)}$ are the test statistics for the LM, RALS-LM(2&3), and RALS-LM(t_5) tests, respectively. (b) $\hat{\rho}^{(2\&3)}_{(2\&3)}$ and $\hat{\rho}^{(2}_{(t_5)}$ indicate the ratio of the estimated error variances for RALS-LM (2&3) and RALS-LM (t_5) tests, respectively. (c) The 1%, 5%, and 10% critical values for the LM test (T = 200) are: -3.61, -3.04, -2.76. (d) The critical values for RALS-LM tests are reported in Table 11.1 of Meng *et al.* (2014). (e) ‡, †, and * represent 1%, 5%, and 10% rejection, respectively.

Categories	Fund	$ au^*_{LM}$	$ au^*_{RALS-LM(2\&3)}$	$\hat{ ho}^{2}_{(2\&3)}$	$\tau^*_{RALS-LM(t_5)}$	$\hat{\rho}^2_{(t_5)}$	\hat{T}_B
Core	ADX	-3.944†	-5.305‡	0.837	-6.167‡	0.703	2002:09
Funds	CET	-5.167‡	-3.632†	0.786	-4.294‡	0.704	2008:09
	CLM	-2.651	-2.064	0.655	-2.409	0.992	2011:08
	CRF	-3.024	-2.113	0.653	-2.445	0.719	2011:08
	FUND	-4.416‡	-4.169‡	0.888	-4.118‡	0.833	2008:11
	GAB	-3.652*	-2.943	0.874	-3.087	0.906	2014:07
	GAM	-5.411‡	-7.033‡	0.616	-6.982‡	0.553	2000:12
	GRF	-3.045	-3.690†	0.819	-3.308*	0.851	2004:04
	RMT	-3.214	-2.910	0.905	-3.150	0.826	2007:05
	RVT	-3.181	-3.390*	0.918	-3.706†	0.759	2007:01
	SOR	-3.473*	-3.855†	0.829	-4.031‡	0.631	2007:01
	SPE	-12.37‡	-21.874‡	0.304	-25.732‡	0.208	2002:06
	ΤY	-4.554‡	-3.362*	0.666	-4.050‡	0.427	2008:12
	USA	-3.867†	-3.676†	0.735	-3.767†	0.485	2001:01
Corp Debt	ICB	-3.478*	-3.902†	0.787	-4.905‡	0.673	2000:12
BBB	INSI	-3.292	-3.708†	0.860	-4.529‡	0.746	2000:11
	MGF	-3.236	-2.865	0.793	-3.475†	0.676	2008:08
	MIN	-2.521	-1.549	0.848	-1.275	0.788	2013:01
	PAI	-3.528*	-2.903	0.846	-3.005	0.836	2008:10
	VBF	-3.499*	-3.740†	0.873	-3.793†	0.782	2015:07
General	DUC	-3.471*	-2.732	0.868	-2.186	0.859	2015:12
Bond	JHI	-2.705	-2.386	0.928	-2.492	0.812	2012:05
	KMM	-2.905	-3.390*	0.871	-3.557†	0.659	2000:12
	KST	-5.226‡	-4.831‡	0.818	-5.534‡	0.724	2001:03
	MCI	-3.901†	-4.755‡	0.855	-4.469‡	0.928	2000:11
	MCR	-3.093	-3.867†	0.828	-4.038†	0.759	2001:01
	MMT	-3.111	-3.130	0.918	-2.759	0.862	2015:08
	MPV	-3.033	-3.575†	0.782	-2.107	0.661	2012:06
	PCM	-3.866†	-4.363‡	0.683	-3.438*	0.778	2006:12
	PIM	-3.120	-3.004	0.812	-3.132*	0.673	2009:03
	РРТ	-3.038	-2.780	0.810	-2.085	0.640	2007:11

Table 6. LM and RALS-LM Test Results with One Trend Break

Note: (a) τ_{LM}^* , $\tau_{RALS-LM(2\&3)}^*$, $\tau_{RALS-LM(t_5)}^*$ are the test statistics for the LM, RALS-LM(2&3), and RALS-LM(t_5) tests with transformation, respectively. (b) $\hat{\rho}_{(2\&3)}^2$ and $\hat{\rho}_{(t_5)}^2$ indicate the ratio of the estimated error variances for RALS-LM (2&3) and RALS-LM (t_5) tests, respectively. (c) \hat{T}_B denote the estimated break point. (d) The 1%, 5%, and 10% critical values for the one break LM test with transformation (T = 200) are: - 4.261, - 3.716, -3.443. (e) The critical values for RALS-LM tests are reported in Table 1 of Meng *et al.* (2017). (f) ‡, †, and * represent 1%, 5%, and 10% rejection, respectively.

Categories	Fund	$ au^*_{LM}$	$\tau^*_{RALS-LM(2\&3)}$	$\hat{ ho}^2_{(2\&3)}$	$\tau^*_{RALS-LM(t_5)}$	$\hat{\rho}_{(t_5)}^2$	Ĩ	Р В
Core	ADX	-8.232‡	-9.235‡	0.878	-9.846‡	0.785	2000:11	2002:09
Funds	CET	-4.416†	-4.314†	0.815	-4.347†	0.656	2008:09	2008:12
	CLM	-6.184‡	-6.208‡	0.869	-6.449‡	0.759	2008:07	2008:10
	CRF	-8.280‡	-9.020‡	0.783	-9.692‡	0.58	2008:07	2008:10
	FUND	-6.953‡	-6.835‡	0.864	-7.321‡	0.751	2004:08	2009:05
	GAB	-6.085‡	-6.398‡	0.810	-6.996‡	0.737	2001:01	2002:09
	GAM	-6.467‡	-7.535‡	0.782	-8.000‡	0.638	2008:09	2008:12
	GRF	-3.165	-3.582	0.830	-3.668*	0.696	2003:05	2003:08
	RMT	-4.612†	-3.731	0.863	-4.091†	0.710	2007:01	2007:12
	RVT	-4.179*	-4.232†	0.899	-4.510‡	0.778	2007:01	2007:11
	SOR	-6.237‡	-7.347‡	0.826	-7.821‡	0.663	2002:09	2003:09
	SPE	-12.88‡	-14.50‡	0.848	-15.91‡	0.705	2001:02	2001:05
	ΤY	-7.074‡	-10.18‡	0.669	-10.80‡	0.505	2008:10	2009:07
	USA	-7.799‡	-8.416‡	0.812	-9.511‡	0.628	2008:07	2008:12
Corp Debt	ICB	-5.830‡	-6.295‡	0.833	-6.743‡	0.722	2008:08	2009:01
BBB	INSI	-5.688‡	-6.217‡	0.953	-6.286‡	0.906	2008:08	2009:02
	MGF	-5.735‡	-5.674‡	0.931	-5.902‡	0.872	2008:08	2009:01
	MIN	-6.039‡	-6.135‡	0.970	-6.165‡	0.928	2013:03	2013:09
	PAI	-3.776	-3.808	0.940	-3.676	0.934	2008:10	2009:02
	VBF	-4.553†	-4.462†	0.919	-4.247†	0.903	2008:08	2009:02
General	DUC	-6.255‡	-6.840‡	0.858	-6.423‡	0.785	2006:01	2009:01
Bond	JHI	-5.442‡	-5.568‡	0.907	-5.699‡	0.844	2011:06	2012:10
	KMM	-5.087‡	-4.787‡	0.936	-4.657‡	0.784	2007:02	2009:01
	KST	-5.582‡	-5.608‡	0.787	-5.431‡	0.779	2000:11	2001:04
	MCI	-5.500‡	-5.823‡	0.959	-5.736‡	0.935	2007:04	2009:04
	MCR	-5.623‡	-5.625‡	0.867	-5.600‡	0.805	2008:08	2009:02
	MMT	-4.009*	-4.110†	0.889	-4.088†	0.812	2013:03	2013:09
	MPV	-4.287†	-4.624‡	0.821	-3.951†	0.723	2006:11	2007:02
	PCM	-5.733‡	-6.424‡	0.726	-5.586‡	0.867	2008:07	2008:10
	PIM	-4.027*	-4.078†	0.802	-3.931†	0.666	2007:09	2007:12
	PPT	-8.188‡	-8.633‡	0.876	-10.02‡	0.641	2007:09	2007:12

Table 7. LM and RALS-LM Test Results with Two Trend Breaks

Note: (a) τ_{LM}^* , $\tau_{RALS-LM(2\&3)}^*$, $\tau_{RALS-LM(t_5)}^*$ are the test statistics for the LM, RALS-LM (2&3), and RALS-LM (t_5) tests with transformation, respectively. (b) $\hat{\rho}_{(2\&3)}^2$ and $\hat{\rho}_{(t_5)}^2$ indicate the ratio of the estimated error variances for RALS-LM (2&3) and RALS-LM (t_5) tests, respectively. (c) \hat{T}_B denote the optimal number of lags and the estimated break points. (d) The 1%, 5%, and 10% critical values for the two breaks LM test with transformation (T = 200) are: - 4.799, - 4.261, - 3.997. (e) The critical values for RALS-LM tests are reported in Table 1 of Meng *et al.* (2017). (f) \ddagger , \ddagger , and * represent 1%, 5%, and 10% rejection, respectively.

Appendix A: Derivation of h(t) in RALS(t_v) Test

Let $\{y_1, y_2, \dots, y_T\}$ be *i.i.d.* observations from a generalized Student's t-distribution with the following pdf:

$$f(y_t; \nu, \mu, \sigma) = \frac{\Gamma\left(\frac{\nu+1}{2}\right)}{\sigma\Gamma\left(\frac{\nu}{2}\right)\sqrt{\nu\pi}} \left(1 + \frac{(y_t - \mu)^2}{\nu\sigma^2}\right)^{-\frac{1}{2}(\nu+1)},$$

where μ is a location parameter, σ is a scale parameter, and ν denotes degrees of freedom. The log-likelihood function is the following.

$$\ln L_T(\nu, \mu, \sigma) = \frac{1}{T} \sum_{t=1}^T \ln f(y_t; \nu, \mu, \sigma)$$

= $\frac{1}{T} \sum_{t=1}^T \left[\ln \Gamma\left(\frac{\nu+1}{2}\right) - \ln \sigma - \ln \Gamma\left(\frac{\nu}{2}\right) - \frac{1}{2} \ln \nu \pi - \frac{\nu+1}{2} \ln \left(1 + \frac{(y_t - \mu)^2}{\nu \sigma^2}\right) \right]$
= $\frac{1}{T} \cdot T \left[\ln \Gamma\left(\frac{\nu+1}{2}\right) - \ln \sigma - \ln \Gamma\left(\frac{\nu}{2}\right) - \frac{1}{2} \ln \nu \pi \right]$
 $- \frac{1}{T} \sum_{t=1}^T \frac{(\nu+1)}{2} \ln \left(\frac{\nu \sigma^2 + (y_t - \mu)^2}{\nu \sigma^2}\right)$

Differentiating $\ln L_T(\cdot)$ with respect to μ yields,

$$\frac{\partial \ln L_T}{\partial \mu} = -\frac{1}{T} \sum_{t=1}^T \frac{(\nu+1)}{2} \left(\frac{\nu \sigma^2}{\nu \sigma^2 + (y_t - \mu)^2} \right) \frac{2(y_t - \mu)(-1)}{\nu \sigma^2}$$
$$= \frac{1}{T} \sum_{t=1}^T \frac{(\nu+1)(y_t - \mu)}{\nu \sigma^2 + (y_t - \mu)^2} = \frac{1}{T} \sum_{t=1}^T h(y_t)$$

The first order condition is $\frac{1}{T}\sum_{t=1}^{T} h(y_t) = 0$. Replacing y_t with $e_t \sim (\mu = 0, \sigma^2 = 1)$, we obtain,

$$h(e_t) = \frac{(\nu+1)e_t}{\nu+e_t^2}$$

where ν is degrees of freedom.

Categories	Fund	$\tau_{RALS(t_3)}$	$\hat{\rho}^2_{(t_2)}$	$\tau_{RALS(t_7)}$	$\hat{\rho}^2_{(t_7)}$	ĥ
Core Funds	ADX	-3.470 [‡]	0.753	-3.476‡	0.792	8
	CET	-2.211	0.612	-2.009	0.646	5
	CLM	-1.878	0.865	-1.684	0.852	10
	CRF	-1.959	0.793	-1.825	0.681	0
	FUND	-2.426*	0.789	-2.688*	0.731	2
	GAB	-3.367 [†]	0.852	-3.274†	0.817	0
	GAM	-3.395‡	0.451	-3.220‡	0.492	9
	GRF	-1.696	0.913	-1.804	0.820	10
	RMT	-1.713	0.819	-1.769	0.825	10
	RVT	-1.740	0.828	-1.846	0.811	7
	SOR	-1.601	0.585	-1.471	0.631	3
	SPE	-4.190 [‡]	0.615	-3.835 [‡]	0.681	1
	TY	-3.851 [‡]	0.385	-3.669 [‡]	0.410	6
	USA	-1.861	0.486	-1.914	0.530	1
Corp Debt BBB	ICB	-4.419 [‡]	0.630	-4.354‡	0.661	7
	INSI	-3.701‡	0.780	-3.904‡	0.756	5
	MGF	-3.027^{\dagger}	0.630	-3.050 [†]	0.622	8
	MIN	-0.878	0.794	-0.766	0.802	5
	PAI	-3.356 [†]	0.829	-3.266 [†]	0.820	8
	VBF	-3.141 [†]	0.847	-3.104 [†]	0.842	3
General Bond	DUC	-0.736	0.753	-0.830	0.752	1
	JHI	-2.145	0.874	-2.138	0.876	1
	KMM	-3.187^{\dagger}	0.676	-3.289 [‡]	0.681	7
	KST	-2.933†	0.631	-2.936†	0.624	10
	MCI	-2.848^{\dagger}	0.979	-2.817^{\dagger}	0.945	2
	MCR	-2.735*	0.831	-2.706*	0.825	1
	MMT	-3.372 [‡]	0.837	-3.486‡	0.847	1
	MPV	-2.809^{\dagger}	0.777	-2.818^{\dagger}	0.722	8
	PCM	-1.749	0.956	-1.409	0.889	4
	PIM	-3.130 [†]	0.594	-3.306‡	0.587	8
	PPT	-1.496	0.684	-1.495	0.672	10

Appendix B: Additional Tables and Figures

Table B1. RALS(t_v) Test Results with Alternative Degrees of Freedom

Note: (a) $\tau_{RALS(t_v)}$ are the test statistics for the RALS (t_v) test. (b) $\hat{\rho}^2_{(t_v)}$ indicates the ratio of the estimated error variances for the RALS (t_v) . (c) We chose the optimal number of lags (\hat{k}) based on the general-to-specific rule with a maximum 10 lags. (d) *, † and ‡ denote a rejection of the null hypothesis of nonstationarity at the 10%, 5% and 1% significance level, respectively. (e) The critical values of RALS tests are dependent on $\hat{\rho}^2$ and were obtained from Hansen (1995).

Categories	Fund	$ au_{LM}$	$\tau_{RALS-LM(2\&3)}$	$\hat{ ho}_{(2\&3)}^2$	$\tau_{RALS-LM(t_5)}$	$\hat{ ho}_{(t_5)}^2$	\hat{T}_B	ƙ
Core Funds	ADX	-1.952	-1.787	0.827	-1.741	0.723	2002:07	8
	CET	-3.531†	-2.671	0.843	-2.806*	0.714	2008:10	8
	CLM	-2.357	-1.906	0.869	-2.831*	0.805	2008:08	0
	CRF	-1.803	-0.886	0.793	-2.123	0.712	2008:08	0
	FUND	-1.480	-1.204	0.861	-0.992	0.776	2007:10	3
	GAB	-2.312	-1.222	0.878	-1.562	0.830	2009:04	1
	GAM	-2.854*	-2.580	0.720	-2.378	0.632	2008:10	9
	GRF	-2.315	-3.467†	0.827	-2.221	0.985	2003:06	9
	RMT	-1.273	-1.672	0.920	-1.401	0.844	2005:12	10
	RVT	-1.505	-1.699	0.914	-1.423	0.814	2009:04	7
	SOR	-2.567	-2.016	0.856	-2.481	0.615	2008:10	6
	SPE	-1.911	-0.614	0.306	-1.211	0.200	2001:02	0
	ΤY	-3.671‡	-3.230†	0.617	-2.896†	0.433	2008:11	6
	USA	-2.564	-1.995	0.773	-2.180	0.590	2008:10	5
Corp Debt	ICB	-2.769*	-2.745*	0.843	-2.935†	0.741	2000:11	1
BBB	INSI	-2.481	-2.060	0.914	-1.698	0.876	2008:08	10
	MGF	-2.135	-2.660*	0.790	-3.094†	0.663	2008:08	8
	MIN	-2.004	-1.570	0.975	-1.466	0.916	2013:04	5
	PAI	-1.936	-1.888	0.922	-1.948	0.878	2009:09	9
	VBF	-3.210†	-3.739‡	0.893	-3.433†	0.832	2003:06	3
General	DUC	-2.202	-1.597	0.914	-1.211	0.781	2008:12	10
Bond	JHI	-2.178	-2.531	0.951	-2.429	0.873	2012:09	1
	KMM	-2.647	-2.503	0.906	-2.406	0.676	2008:10	7
	KST	-2.035	-1.746	0.713	-1.520	0.726	2000:12	10
	MCI	-2.546	-2.884*	0.927	-2.426	0.978	2009:04	2
	MCR	-2.836*	-2.646	0.879	-2.258	0.847	2014:11	10
	MMT	-2.794*	-2.541	0.950	-2.280	0.856	2008:08	1
	MPV	-2.734	-2.822*	0.824	-1.990	0.772	2006:12	8
	PCM	-3.078†	-3.085†	0.820	-2.450	0.905	2008:08	8
	PIM	-3.546†	-3.566‡	0.794	-3.832‡	0.614	2007:09	8
	PPT	-3.143†	-3.059†	0.834	-3.335†	0.582	2007:10	10

Table B2. LM and RALS-LM Test Results with One Level Shift

Note: (a) τ_{LM} , $\tau_{RALS-LM(2\&3)}$, $\tau_{RALS-LM(t_5)}$ are the test statistics for the LM, RALS-LM(2&3), and RALS-LM(t_5) tests, respectively. (b) $\hat{\rho}^2_{(2\&3)}$ and $\hat{\rho}^2_{(t_5)}$ indicate the ratio of the estimated error variances for RALS-LM(2&3) and RALS-LM(t_5) tests, respectively. (c) \hat{k} and \hat{T}_B denote the optimal number of lags and the estimated break point, respectively. Since the number of lags and the break date determined using max F statistic are used in both LM and RALS-LM unit root tests, we report them one time. (d) The critical values for LM and RALS-LM tests are reported in Table 11.1 of Meng *et al.* (2014). (e) *, †, and ‡ denote a 10%, 5%, and 1% rejection, respectively.

Categories	Fund	$\tau_{RALS-LM(t_3)}$	$\hat{ ho}_{(t_3)}^2$	$\tau_{RALS-LM(t_7)}$	$\hat{ ho}_{(t_7)}^2$	\widehat{T}_B	ƙ
Core Funds	ADX	-1.911	0.695	-1.649	0.740	2002:07	8
	CET	-3.012†	0.702	-2.874*	0.725	2008:10	8
	CLM	-1.954	0.850	-1.848	0.817	2008:08	0
	CRF	-2.066	0.789	-2.124	0.679	2008:08	0
	FUND	-0.717	0.829	-0.776	0.785	2007:10	3
	GAB	-2.179	0.864	-2.075	0.856	2009:04	1
	GAM	-2.371	0.635	-2.373	0.635	2008:10	9
	GRF	-2.144	0.994	-2.052	0.947	2003:06	9
	RMT	-1.322	0.848	-1.463	0.843	2005:12	10
	RVT	-1.336	0.832	-1.479	0.809	2009:04	7
	SOR	-2.859†	0.589	-2.525	0.654	2008:10	6
	SPE	-1.025	0.210	-0.843	0.201	2001:02	0
	ΤY	-2.849†	0.415	-2.755†	0.444	2008:11	6
	USA	-1.997	0.575	-1.992	0.605	2008:10	5
Corp Debt BBB	ICB	-2.578	0.730	-2.478	0.755	2000:11	1
	INSI	-2.143	0.905	-2.128	0.876	2008:08	10
	MGF	-3.004†	0.669	-3.128†	0.663	2008:08	8
	MIN	-1.487	0.896	-1.462	0.927	2013:04	5
	PAI	-1.681	0.875	-1.724	0.892	2009:09	9
	VBF	-3.399†	0.833	-3.457†	0.835	2003:06	3
General Bond	DUC	-1.597	0.757	-1.683	0.778	2008:12	10
	JHI	-2.443	0.854	-2.434	0.881	2012:09	1
	KMM	-2.383	0.661	-2.419	0.689	2008:10	7
	KST	-1.419	0.777	-1.606	0.701	2000:12	10
	MCI	-2.448	0.977	-2.409	0.976	2009:04	2
	MCR	-2.676	0.860	-2.612	0.839	2014:11	10
	MMT	-2.247	0.836	-2.306	0.867	2008:08	1
	MPV	-2.125	0.834	-1.910	0.733	2006:12	8
	PCM	-2.059	0.924	-1.933	0.888	2008:08	8
	PIM	-3.797‡	0.617	-3.851‡	0.617	2007:09	8
	PPT	-3.434‡	0.545	-3.274†	0.605	2007:10	10

Table B2. Continued

Note: (a) $\tau_{RALS-LM(t_3)}$, $\tau_{RALS-LM(t_7)}$ are the test statistics for the RALS-LM tests with degrees of freedom of 3 and 7, respectively. (b) $\hat{\rho}_{(t_3)}^2$ and $\hat{\rho}_{(t_7)}^2$ indicate the ratio of the estimated error variances for RALS-LM (t_3) and RALS-LM (t_7) tests, respectively. (c) \hat{k} and \hat{T}_B denote the optimal number of lags and the estimated break point, respectively. Since the number of lags and the break date determined using *max F* statistic are used in both LM and RALS-LM unit root tests, we report them one time. (d) The critical values for RALS-LM tests are reported in Table 11.1 of Meng *et al.* (2014). (e) *, †, and ‡ denote a 10%, 5%, and 1% rejection, respectively.

Categories	Fund	$ au_{LM}$	$\tau_{RALS-LM(2\&3)}$	$\hat{ ho}_{(2\&3)}^2$	$\tau_{RALS-LM(t_5)}$	$\hat{ ho}_{(t_5)}^2$	\widehat{T}_{I}	3	ƙ
Core	ADX	-1.780	-1.356	0.875	-1.499	0.772	2002:07	2007:11	8
Funds	CET	-3.180†	-2.887*	0.839	-3.361†	0.684	2001:01	2008:10	5
	CLM	-2.163	-1.981	0.871	-2.598	0.825	2008:08	2010:01	0
	CRF	-2.118	-2.172	0.880	-2.788*	0.801	2002:09	2008:08	0
	FUND	-1.523	-1.081	0.893	-0.910	0.773	2007:10	2009:02	4
	GAB	-2.453	-1.654	0.857	-2.213	0.861	2008:11	2009:04	7
	GAM	-2.658	-3.289†	0.752	-3.341†	0.620	2008:10	2008:12	9
	GRF	-3.474†	-3.897‡	0.812	-3.895‡	0.698	2003:05	2004:03	1
	RMT	-1.194	-0.699	0.949	-0.997	0.898	2008:12	2009:04	10
	RVT	-1.903	-2.112	0.932	-1.850	0.828	2008:08	2009:04	7
	SOR	-2.127	-1.960	0.858	-2.067	0.675	2008:10	2008:12	6
	SPE	-2.010	-0.851	0.289	-1.478	0.198	2001:02	2009:12	0
	ΤY	-2.024	-1.489	0.654	-0.297	0.464	2008:11	2009:02	10
	USA	-2.579	-2.367	0.813	-1.773	0.630	2004:04	2008:10	0
Corp Debt	ICB	-2.982*	-2.911*	0.858	-3.233†	0.736	2000:11	2008:11	1
BBB	INSI	-1.856	-1.384	0.937	-0.929	0.811	2008:08	2009:01	1
	MGF	-2.342	-2.826*	0.803	-3.508‡	0.677	2008:08	2008:10	8
	MIN	-1.412	-1.033	0.981	-1.039	0.907	2010:11	2013:04	5
	PAI	-2.600	-2.880*	0.959	-2.909*	0.926	2008:12	2009:09	9
	VBF	-3.406†	-3.665‡	0.916	-3.719‡	0.835	2003:06	2008:12	6
General	DUC	-3.173†	-3.018†	0.905	-1.976	0.815	2006:02	2008:12	1
Bond	JHI	-2.309	-2.467	0.977	-2.286	0.918	2011:07	2012:09	1
	KMM	-2.540	-2.499	0.931	-2.647*	0.631	2000:11	2008:10	7
	KST	-2.289	-2.042	0.761	-2.110	0.791	2000:12	2001:07	10
	MCI	-2.673	-3.066†	0.939	-2.661	0.991	2008:09	2009:04	2
	MCR	-2.341	-1.723	0.886	-1.513	0.859	2008:08	2014:11	10
	MMT	-3.126†	-3.239†	0.956	-3.078†	0.874	2008:08	2008:12	1
	MPV	-2.202	-1.971	0.872	-1.692	0.819	2003:11	2006:12	10
	PCM	-2.078	-2.044	0.888	-2.101	0.895	2007:02	2008:08	4
	PIM	-3.389†	-3.222†	0.787	-3.455‡	0.605	2007:09	2008:09	8
	PPT	-2.759	-2.275	0.827	-2.098	0.563	2007:10	2008:09	10

Table B3. LM and RALS-LM Test Results with Two Level Shifts

Note: (a) τ_{LM} , $\tau_{RALS-LM(2\&3)}$, $\tau_{RALS-LM(t_5)}$ are the test statistics for the LM, RALS-LM (2&3), and RALS-LM (t_5) tests, respectively. (b) $\hat{\rho}^2_{(2\&3)}$ and $\hat{\rho}^2_{(t_5)}$ indicate the ratio of the estimated error variances for RALS-LM (2&3) and RALS-LM (t_5) tests, respectively. (c) \hat{k} and \hat{T}_B denote the optimal number of lags and the estimated break points, respectively. Since the number of lags and the break dates determined using max F statistic are used in both LM and RALS-LM unit root tests, we report them one time. (d) The critical values for LM and RALS-LM tests are reported in Table 11.1 of Meng *et al.* (2014). (e) *, †, and ‡ denote a 10%, 5%, and 1% rejection, respectively.

Categories	Fund	$\tau_{RALS-LM(t_3)}$	$\hat{ ho}_{(t_3)}^2$	$\tau_{RALS-LM(t_7)}$	$\hat{\rho}^2_{(t_7)}$	Î	B	ƙ
Core Funds	ADX	-1.668	0.747	-1.410	0.787	2002:07	2007:11	8
	CET	-3.386†	0.668	-3.328†	0.696	2001:01	2008:10	5
	CLM	-1.901	0.858	-1.764	0.842	2008:08	2010:01	0
	CRF	-2.682*	0.835	-2.840*	0.782	2002:09	2008:08	0
	FUND	-0.342	0.814	-0.487	0.819	2007:10	2009:02	4
	GAB	-3.021*	0.971	-2.923*	0.917	2008:11	2009:04	7
	GAM	-3.402†	0.603	-3.291†	0.633	2008:10	2008:12	9
	GRF	-2.732*	0.714	-2.807*	0.669	2003:05	2004:03	1
	RMT	-0.938	0.882	-1.027	0.903	2008:12	2009:04	10
	RVT	-1.767	0.834	-1.897	0.830	2008:08	2009:04	7
	SOR	-2.210	0.670	-2.140	0.702	2008:10	2008:12	6
	SPE	-1.331	0.206	-1.074	0.200	2001:02	2009:12	0
	ΤY	-0.897	0.454	-1.272	0.480	2008:11	2009:02	10
	USA	-1.291	0.610	-1.455	0.635	2004:04	2008:10	0
Corp Debt BBB	ICB	-2.790*	0.720	-2.707*	0.746	2000:11	2008:11	1
	INSI	-0.985	0.812	-1.106	0.834	2008:08	2009:01	1
	MGF	-3.465‡	0.676	-3.523‡	0.681	2008:08	2008:10	8
	MIN	-1.072	0.889	-1.023	0.919	2010:11	2013:04	5
	PAI	-2.417	0.955	-2.504	0.945	2008:12	2009:09	9
	VBF	-3.199†	0.855	-3.257†	0.858	2003:06	2008:12	6
General Bond	DUC	-1.811	0.791	-2.083	0.823	2006:02	2008:12	1
	JHI	-2.288	0.907	-2.293	0.923	2011:07	2012:09	1
	KMM	-2.742*	0.585	-2.595*	0.663	2000:11	2008:10	7
	KST	-1.997	0.843	-2.189	0.762	2000:12	2001:07	10
	MCI	-2.654	0.997	-2.668	0.986	2008:09	2009:04	2
	MCR	-1.752	0.871	-1.675	0.849	2008:08	2014:11	10
	MMT	-3.034†	0.859	-3.101†	0.884	2008:08	2008:12	1
	MPV	-1.948	0.834	-1.817	0.804	2003:11	2006:12	10
	PCM	-2.050	0.928	-2.133	0.875	2007:02	2008:08	4
	PIM	-3.408†	0.603	-3.484‡	0.613	2007:09	2008:09	8
	PPT	-2.176	0.510	-2.072	0.592	2007:10	2008:09	10

Table B3. Continued

Note: (a) $\tau_{RALS-LM(t_3)}$, $\tau_{RALS-LM(t_7)}$ are the test statistics for the RALS-LM tests with degrees of freedom of 3 and 7, respectively. (b) $\hat{\rho}^2_{(t_3)}$ and $\hat{\rho}^2_{(t_7)}$ indicate the ratio of the estimated error variances for RALS-LM (t_3) and RALS-LM (t_7) tests, respectively. (c) \hat{k} and \hat{T}_B denote the optimal number of lags and the estimated break points, respectively. Since the number of lags and the break dates determined using *max F* statistic are used in both LM and RALS-LM unit root tests, we report them one time. (d) The critical values for RALS-LM tests are reported in Table 11.1 of Meng *et al.* (2014). (e) *, †, and ‡ denote a 10%, 5%, and 1% rejection, respectively.

Categories	Fund	$\tau_{RALS-LM(t_3)}$	$\hat{ ho}_{(t_3)}^2$	$ au_{RALS-LM(t_7)}$	$\hat{ ho}_{(t_7)}^2$	ƙ
Core Funds	ADX	-2.086	0.751	-2.153	0.793	8
	CET	-2.372	0.614	-2.134	0.651	5
	CLM	-1.388	0.890	-1.179	0.874	10
	CRF	-1.909	0.624	-1.604	0.557	0
	FUND	-1.574	0.802	-1.737	0.750	2
	GAB	-3.571‡	0.853	-3.481†	0.819	0
	GAM	-4.121‡	0.453	-3.965‡	0.493	9
	GRF	-2.142	0.915	-2.310	0.814	10
	RMT	-0.937	0.828	-0.997	0.832	10
	RVT	-1.234	0.833	-1.344	0.817	7
	SOR	-2.171	0.583	-1.987	0.634	3
	SPE	-6.225‡	0.235	-6.400‡	0.230	3
	TY	-2.944†	0.342	-2.538*	0.378	4
	USA	-1.587	0.490	-1.660	0.533	1
Corp Debt BBB	ICB	-4.311‡	0.633	-4.254‡	0.664	7
	INSI	-3.897‡	0.786	-4.112‡	0.757	5
	MGF	-3.515‡	0.624	-3.516‡	0.616	8
	MIN	-0.849	0.802	-0.747	0.810	5
	PAI	-2.658	0.801	-2.515	0.808	8
	VBF	-2.965*	0.848	-2.952*	0.845	3
General Bond	DUC	-2.463	0.825	-2.397	0.825	3
	JHI	-2.046	0.870	-2.028	0.874	1
	KMM	-2.491	0.695	-2.569	0.702	7
	KST	-2.320	0.740	-2.444	0.679	10
	MCI	-2.817*	0.985	-2.792*	0.949	2
	MCR	-2.257	0.802	-2.207	0.794	1
	MMT	-3.206†	0.835	-3.301†	0.849	1
	MPV	-2.841*	0.771	-2.864*	0.720	8
	PCM	-1.281	0.929	-1.044	0.866	4
	PIM	-3.037†	0.579	-3.173†	0.580	8
	PPT	-1.557	0.630	-1.511	0.639	10

Table B4. No Trend Break RALS-LM Test Results with Alternative Degrees of Freedom

Note: (a) $\tau_{RALS-LM(t_3)}$, $\tau_{RALS-LM(t_7)}$ are the test statistics for the RALS-LM tests with degrees of freedom of 3 and 7, respectively. (b) $\hat{\rho}^2_{(t_3)}$ and $\hat{\rho}^2_{(t_7)}$ indicate the ratio of the estimated error variances for RALS-LM (t_3) and RALS-LM (t_7) tests, respectively. (c) \hat{k} denotes the optimal number of lags. Since the number of lags determined using max F statistic is used in both LM and RALS-LM unit root tests, we report this one time. (d) The critical values for RALS-LM tests are reported in Table 11.1 of Meng *et al.* (2014). (e) \ddagger , \dagger , and \ast represent 1%, 5%, and 10% rejection, respectively.

Categories	Fund	$\tau^*_{RALS-LM(t_3)}$	$\hat{ ho}_{(t_3)}^2$	$\tau^*_{RALS-LM(t_7)}$	$\hat{ ho}_{(t_7)}^2$	\widehat{T}_B	ƙ
Core Funds	ADX	-6.331‡	0.671	-6.050‡	0.724	2002:09	8
	CET	-3.492†	0.733	-3.416*	0.711	2008:09	10
	CLM	-2.248	0.993	-2.100	0.980	2011:08	8
	CRF	-2.630	0.741	-2.313	0.697	2011:08	0
	FUND	-3.156	0.887	-3.121	0.855	2008:11	4
	GAB	-3.177	0.931	-3.028	0.889	2014:07	0
	GAM	-6.958‡	0.543	-6.981‡	0.561	2000:12	9
	GRF	-3.158	0.920	-3.417*	0.806	2004:04	10
	RMT	-3.085	0.839	-3.182	0.824	2007:05	10
	RVT	-3.664†	0.731	-3.601†	0.763	2007:01	4
	SOR	-3.729†	0.641	-3.817†	0.651	2007:01	6
	SPE	-15.23‡	0.207	-14.581‡	0.213	2002:06	0
	TY	-4.052‡	0.402	-3.682†	0.442	2008:12	3
	USA	-2.664	0.491	-2.643	0.517	2001:01	6
Corp Debt BBB	ICB	-4.946‡	0.660	-4.884‡	0.667	2000:12	7
	INSI	-4.513‡	0.751	-4.523‡	0.747	2000:11	5
	MGF	-3.516†	0.687	-3.426†	0.675	2008:08	8
	MIN	-0.886	0.777	-0.786	0.789	2013:01	3
	PAI	-2.561	0.870	-2.443	0.855	2008:10	8
	VBF	-3.772†	0.794	-3.781†	0.803	2015:07	3
General Bond	DUC	-2.081	0.881	-1.997	0.845	2015:12	3
	JHI	-2.540	0.791	-2.473	0.824	2012:05	1
	KMM	-3.560†	0.663	-3.552†	0.663	2000:12	7
	KST	-5.510‡	0.749	-5.527‡	0.712	2001:03	10
	MCI	-4.449‡	0.934	-4.494‡	0.919	2000:11	2
	MCR	-3.994†	0.775	-4.050‡	0.755	2001:01	1
	MMT	-2.715	0.855	-2.794	0.865	2015:08	1
	MPV	-2.424	0.686	-2.402	0.650	2012:06	8
	PCM	-2.473	0.828	-2.535	0.792	2006:12	9
	PIM	-2.807	0.694	-3.010	0.670	2009:03	9
	PPT	-1.566	0.626	-1.631	0.632	2007:11	9

Table B5. One Trend Break RALS-LM Test Results with Alternative Degrees of Freedom

Note: (a) $\tau_{RALS-LM(t_3)}^*$, $\tau_{RALS-LM(t_7)}^*$ are the test statistics for the RALS-LM tests with degrees of freedom of 3 and 7, respectively. (b) $\hat{\rho}_{(t_3)}^2$ and $\hat{\rho}_{(t_7)}^2$ indicate the ratio of the estimated error variances for RALS-LM (t_3) and RALS-LM (t_7) tests, respectively. (c) \hat{k} and \hat{T}_B denote the optimal number of lags and the estimated break point, respectively. Since the number of lags and the break date determined using *max F* statistic are used in both LM and RALS-LM unit root tests, we report them one time. (d) The critical values for RALS-LM tests are reported in Table 1 of Meng *et al.* (2017). (e) \ddagger , \ddagger , and \ast represent 1%, 5%, and 10% rejection, respectively.

Categories	Fund	$\tau^*_{RALS-LM(t_3)}$	$\hat{\rho}^2_{(t_3)}$	$\tau^*_{RALS-LM(t_7)}$	$\hat{\rho}^2_{(t_7)}$	\widehat{T}_{I}	3	ƙ
Core Funds	ADX	-9.938‡	0.764	-9.772‡	0.799	2000:11	2002:09	8
	CET	-4.319†	0.637	-4.356†	0.670	2008:09	2008:12	5
	CLM	-5.257‡	0.812	-5.547‡	0.767	2008:07	2008:10	0
	CRF	-9.526‡	0.581	-9.795‡	0.579	2008:07	2008:10	0
	FUND	-6.289‡	0.797	-6.164‡	0.807	2004:08	2009:05	4
	GAB	-6.936‡	0.749	-7.039‡	0.728	2001:01	2002:09	0
	GAM	-7.991‡	0.614	-7.986‡	0.654	2008:09	2008:12	9
	GRF	-3.458	0.739	-3.753*	0.683	2003:05	2003:08	6
	RMT	-3.370	0.693	-3.184	0.732	2007:01	2007:12	1
	RVT	-4.429†	0.780	-4.366†	0.783	2007:01	2007:11	9
	SOR	-5.018‡	0.612	-4.884‡	0.651	2002:09	2003:09	0
	SPE	-16.43‡	0.672	-15.94‡	0.718	2001:02	2001:05	5
	ΤY	-10.75‡	0.483	-10.62‡	0.524	2008:10	2009:07	6
	USA	-8.181‡	0.690	-7.916‡	0.717	2008:07	2008:12	10
Corp Debt BBB	ICB	-6.896‡	0.696	-6.665‡	0.736	2008:08	2009:01	7
1	INSI	-6.495‡	0.932	-6.659‡	0.913	2008:08	2009:02	5
	MGF	-5.612‡	0.865	-5.529‡	0.877	2008:08	2009:01	8
	MIN	-6.158‡	0.914	-6.171‡	0.936	2013:03	2013:09	5
	PAI	-3.432	0.951	-3.480	0.942	2008:10	2009:02	8
	VBF	-4.232†	0.91	-4.263†	0.901	2008:08	2009:02	3
General Bond	DUC	-6.225‡	0.778	-6.151‡	0.809	2006:01	2009:01	3
	JHI	-5.488‡	0.828	-5.457‡	0.849	2011:06	2012:10	1
	KMM	-4.287†	0.803	-4.393†	0.797	2007:02	2009:01	7
	KST	-5.422‡	0.831	-5.419‡	0.749	2000:11	2001:04	10
	MCI	-5.721‡	0.938	-5.741‡	0.933	2007:04	2009:04	2
	MCR	-5.223‡	0.803	-5.137‡	0.808	2008:08	2009:02	1
	MMT	-4.094†	0.795	-4.092†	0.820	2013:03	2013:09	1
	MPV	-3.928†	0.748	-3.998†	0.707	2006:11	2007:02	8
	PCM	-5.480‡	0.892	-5.651‡	0.854	2008:07	2008:10	4
	PIM	-3.768*	0.679	-4.022†	0.664	2007:09	2007:12	8
	PPT	-10.53‡	0.576	-9.777‡	0.676	2007:09	2007:12	10

Table B6. Two Trend Break RALS-LM Test Results with Alternative Degrees of Freedom

Note: (a) $\tau_{RALS-LM(t_3)}^*$, $\tau_{RALS-LM(t_7)}^*$ are the test statistics for the RALS-LM tests with degrees of freedom of 3 and 7, respectively. (b) $\hat{\rho}_{(t_3)}^2$ and $\hat{\rho}_{(t_7)}^2$ indicate the ratio of the estimated error variances for RALS-LM (t_3) and RALS-LM (t_7) tests, respectively. (c) \hat{k} and \hat{T}_B denote the optimal number of lags and the estimated break points, respectively. Since the number of lags and the break dates determined using max F statistic are used in both LM and RALS-LM unit root tests, we report them one time. (d) The critical values for RALS-LM tests are reported in Table 1 of Meng *et al.* (2017). (e) \ddagger, \dagger , and * represent 1%, 5%, and 10% rejection, respectively.

Appendix C: Additional Figures

Figure C1: Discount Data with Estimated Time-Varying Intercepts and Trend



(a) Core Funds



(b) Core Debt BBB Funds



(c) General Bond Funds







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