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AUWP 2013-08

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A nonparametric study of real exchange rate persistence over a century^{*}

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July 2013

Abstract

This paper estimates the degree of persistence of 16 long-horizon real exchange rates relative to the US dollar. We use nonparametric operational algorithms by El-Gamal and Ryu (2006) for general nonlinear models based on two statistical notions: the short memory in mean (SMM) and the short memory in distribution (SMD). We found substantially shorter maximum half-life (MHL) estimates than the counterpart from linear models, which is robust to the choice of bandwidth with exceptions of Canada and Japan.

JEL Classification: C14; C15; C22; F31; F41

Keywords: Real Exchange Rate; Purchasing Power Parity; Short Memory in Mean; Short-

Memory in Distribution; ϕ -mixing; Max Half-Life; Max Quarter-Life

^{*} Madeline Kim provided excellent research assistance.

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I Introduction

This paper measures the persistence of the real exchange rate using a nonlinear nonparametric approach developed by El-Gamal and Ryu (2006) for 16 long-horizon real exchange rates of developed countries relative to the US dollar.

Taylor (2002) constructed over a hundred-year long real exchange rates for 20 countries. Implementing an array of *linear* unit root tests, he reported very strong evidence in favor of purchasing power parity (PPP), which was later questioned by Lopez, Murray, and Papell (2005) who pointed out that his results were not robust to the choice of lag selection methods. Kim and Moh (2010), however, employed a nonlinear unit root test by Park and Shintani (2005, 2012) that allowed an array of transition functions for Taylor's (2002) data, finding very strong evidence of nonlinear PPP.

Even though the current literature finds fairly strong evidence for PPP from long-horizon real exchange rates, the profession fails to find persuasive answers to the so-called PPP puzzle (Rogoff, 1996), which states that the 3- to 5-year consensus half-life, based on *linear* models, seems too large to be reconciled by highly volatile short-run exchange rate dynamics.

Murray and Papell (2002) and Rossi (2005), for example, report half-lives with wide confidence intervals that extend to positive infinity. Panel estimations often provide substantially shorter half-lives than the consensus half-life, however, Murray and Papell (2005) reported similarly long half-life estimates from panel models correcting for small-sample bias.¹

¹ One related issue of aggregation bias was raised by Imbs, Mumtaz, Ravn, and Rey (2005), who point out that PPP puzzle might be caused by aggregation bias which neglects sectoral

As shown by Taylor (2001), half-life estimates from linear models tend to be biased upward when the true data generating process (DGP) is nonlinear. However, it is not straightforward how to measure the persistence from nonlinear models, because popularly used nonlinear models are state-dependent stochastic processes. That is, the half-life from these models depends upon the current state and the size of the shock.

One may estimate the persistence of the real exchange rate only in regimes outside the inaction band, that is, subsets of the full sample, which is not fully comparable to half-life measures from linear models based on the full sample. Rigorous methods include Gallant, Rossi, and Tauchen (1993), Koop, Pesaran, and Potter (1996), and Potter (2000) who proposed nonlinear analogs of impulseresponse functions. See, among others, Baum, Barkoulas, and Caglayan (2001) and Lothian and Taylor (2008) for research work that employ such methods. Shintani (2006) also proposed a nonparametric method based on the largest Lyapunov exponent of the series to evaluate the speed of adjustment in presence of nonlinearities, finding fairly shorter half-lives than the consensus half-life.

This paper uses a nonlinear nonparametric approach proposed by El-Gamal and Ryu (2006) that employs more general time series notions of the convergence toward the long-run equilibrium: short-memory-in-mean (SMM) and shortmemory-in-distribution (SMD) as an alternative to the stationarity in linear model framework (Granger and Teräsvirta, 1993; Granger, 1995). SMM and SMD nest linear models as a special case.

heterogeneity in convergence rates, while Chen and Engel (2005), Parsley and Wei (2007), Crucini and Shintani (2008), and Broda and Weinstein (2008) have found negligible aggregation biases.

Our nonparametric approach does not require the knowledge on the parametric representation of transition functions nor any distributional assumptions, so our results are less likely to be influenced by specification errors. In what follows, we provide straightforward algorithms to measure the persistence not only for the first moment (SMM), but also for the entire distribution (SMD). That is, after estimating conditional and unconditional densities by kernel methods, we measure the rate of convergence by using metrics for SMM and SMD based on a worst-case scenario.

Using long-horizon real exchange rates for 16 currencies *vis-à-vis* the US dollar, we find substantially low half-lives using notions of SMM and SMD with exceptions of Canada and Japan. Especially, our maximum half-life estimates for SMM are substantially lower than those from linear models. Our estimates for SMD add new insights to the current literature in favor of a century-long PPP. We also report maximum quarter-life estimates (Steinsson, 2008) to study monotonicity of convergence over time.

We also note that our results provide interesting contrast compared with those of El-Gamal and Ryu (2006) who used five short-horizon current float (post Bretton Woods) exchange rates relative to the US dollar. Their estimates tend to exhibit very slow convergence rates, which may imply indefinitely long half-lives, as the bandwidth parameter increases, even though their half-life estimates are similar to ours when fairly wide bandwidth window is used. This may indicate that utilizing long-horizon data might be crucially important to help understand the PPP puzzle.

The remainder of the paper is organized as follows. Section 2 presents our baseline methodologies and operational algorithms for estimating convergence

rates using our key statistical notions. In Section 3, we describe the data and report major empirical findings. Section 4 concludes.

II The Econometric Model

This section presents some useful definitions for our nonparametric model as an alternative to conventional linear models that are often employed in the current empirical international economics literature. We also provide our nonparametric measures of persistence for a general Markovian univariate time series models.

Let e_t be the natural logarithm nominal exchange rate as the domestic currency (US dollar) price of the foreign currency. p_t and p_t^* denote the price level in the home (US) and the foreign country, respectively, in natural logarithms. When e_t , p_t^* , and p_t are individually integrated (nonstationary) processes, but are cointegrated with the cointegrating vector [1, 1, -1], the real exchange rate, $x_t = e_t + p_t - p_t^*$, is a weakly stationary process, which is consistent with the conventional linear model for PPP. It is convenient to use an autoregressive process for x_t to measure the persistence of PPP deviations as follows.

$$x_{t+1} = \rho x_t + \varepsilon_{t+1},$$

where deterministic terms are omitted for simplicity and ρ is the persistence parameter bounded by 1 from above.

Alternatively, we consider the following representation for x_t which nests the previous linear representation as a special case.

$$x_{t+1} = m(x_t) + \varepsilon_{t+1}$$

Note that this equation implies $m(x_t)$ is the conditional expectation of x_{t+1} at time t given information set. The present paper extends this nonlinear representation into a general framework that extends more than the first moment.

We employ nonparametric measures of persistence for general non-linear model, which is based on the framework proposed by El-Gamal and Ryu (2006) for a first-order Markovian univariate time series $\{x_t\}$. Abandoning linearity in time series domain, we pursue nonlinearity in density domain instead. From the Chapman-Kolmogorov equations, we define transition probability kernel and the Markov operator, which can be approximated by a finite transition matrix. We also directly apply the consistent tests of ergodicity and mixing to our relative stock index data via Domowitz and El-Gamal (1993, 1996, 2001).

As stated in El-Gamal and Ryu (2006), we defined short memory in distribution (SMD) and the short memory in mean (SMM) as follows. The time series is said to have *Short Memory in Distribution* (SMD) property if $F_s(x) \Rightarrow \overline{F}(x)$, as $s \uparrow \infty$ where $F_s(x) = \Pr(x_{t+s} \le x \mid A_t)$ is the cumulative distribution function of x_{t+s} conditional on the past information set $A_t = \sigma(x_{t-j}; j \ge 0)$, and \overline{F} be some fixed (unconditional) distribution function. The time series is said to have *Short Memory in Mean* (SMM) property if $||E[x_{t+s} \mid A_t] - E[x_{t+s}]|| < c_s; c_s \xrightarrow{s\uparrow\infty} 0.^2$

We use the asymptotic independence notion of uniform or ϕ -mixing to study SMD and SMM. As shown by El-Gamal and Ryu (2006), we can calculate the SMD and SMM numerically. That is, we can get the finite grid analog $\phi_n(s)$ which converges to $\phi(s)$ as the grid size $n \uparrow \infty$. Similarly, we can also get the *grid*

² Note that SMM is equivalent to *mixing in mean* or *mixingales* as discussed in McLeish (1978) and Gallant and White (1988), while SMD shares a property of mixing.

 $MDM_n(s)$ which converges to the Maximum Distance in Mean, MDM(s), the measure of SMM, as the grid size $n \uparrow \infty$. For the detailed explanations on the numerical algorithms to compute our persistence measures and convergence arguments of finite grids of SMD and SMM, see El-Gamal and Ryu (2006).

The notion of half-life can now be replaced by the value of *s* at which $MDM_n(s) = 0.5 \times MDM_n(0)$, that is, the number of periods needed for the worst possible transitory shock from the unconditional mean to be cut in half. This notion may then be extended beyond half-life to consider *Max m-life* as the number of time periods before the worst possible shock would have shrunk to (1-*m*) of its original magnitude. Likewise, we define *Max quarter-life* by the number of time periods before the worst possible shock would have shrunk to 0.25, i.e., *m* = 0.75 of its initial one unit shock.³

For non-parametric estimation of $P_{T,n}$ using a kernel estimator, we begin with the estimated $\phi(s)$ and *Max m-life* using so-called Silverman's rule of thumb $h_T = \sigma_T T^{-1/5}$, where σ_T is the standard deviation of our series. The estimated *Max m-life* with this bandwidth selection rule typically yielded quite less persistent dynamics which is in favor of the PPP hypothesis. However, as El-Gamal and Ryu (2006) shows, such results may not be reliable because this selection rule tends to produce an over-smoothed estimate of the transition density, which results in downward bias in the estimates of $\phi(s)$ and *Max m-life*. Therefore, the rule of thumb tends to yield empirical support for the long-term PPP hypothesis.

³ This metric is an extension of the quarter-life that is introduced by Steinsson (2008), which is based on linear regression models. This additional measure of persistence can be used to see if the convergence takes place monotonically.

Realizing this issue, we implement estimations for an array of the choice of the level of under-smoothing, *k*. That is, we modify the Silverman's rule of thumb as follows.

$$h_T = \left(\frac{\sigma_T}{k}\right) T^{-1/5}$$

And we report our estimation results for *k* ranging 1 to 10. We note our estimates for $\phi(s)$ (or *Max m-life*) often converge each other as *k* approaches to 10. We interpret such results as empirical findings that support the validity of the PPP hypothesis. However, we note that the time series not converging each other as k approaches to 10 or converging each other with exceeding 4~5 years of max-half-life does not support the PPP hypothesis.

III Empirical Results

We extended Taylor's (2002) over hundred-year long real exchange rates for 16 developed countries relative to the US dollar by adding observations through 2004 for non-Eurozone countries from the IFS CD-ROM. For Eurozone countries, the sample period ends in 1998. We omitted 4 less developed countries. The data frequency is annual and all exchange rates are CPI-based rates with an exception of Portugal, which is based on the GDP deflator.

In Table 1, we first report benchmark estimates for the half-life from a linear model. We chose the number of lags by the general-to-specific rule with a maximum 6 lags. It is well-known that the least squares estimator for the persistence parameter in autoregressive models is biased when deterministic terms are present. We correct for median bias using Hansen's (1999) grid bootstrap method.

Overall, we find evidence that is consistent with the PPP puzzle from the linear model. We obtain very long half-life point estimates ranging from 2.049 years for Finland to positive infinity for Japan and Switzerland. 95% lower-bound estimates range from 1.282 to 19.204 years, while upper-bounds extend to positive infinity for 9 out of 16 currencies.

This seemingly sluggish rate of adjustment, however, does not necessarily imply strong evidence of the PPP puzzle, because as Taylor (2001) points out, if the true DGP is nonlinear, statistical inferences based on the linear model framework are not reliable due to specification errors. In what follows, we present substantially faster convergence rates based on our nonparametric nonlinear models for the real exchange rate.

Table I around here

We next implement statistical tests for ergodicity and mixing, proposed by Domowitz and El-Gamal (2001), for our exchange rates. For this purpose, unit root processes are reformulated as a general ergodic failure in a *nonlinear* first-order Markovian univariate process. The test rejects the null hypothesis of ergodicity if the *p*-value of a single randomized test is smaller than a pre-specified value. We then determine the rejection of ergodicity null by the percentiles of the density of *p*-values which are less than or close to a pre-specified number, e.g., 5%.

Our randomized test fails to reject the null of mixing for all countries with exceptions of Japan and Norway of which the percentile of *p*-values are substantially different from pre-specified values, which is consistent with

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empirical findings of nonlinear mean reversion via the inf-*t* test from Kim and Moh (2010). In contrast, we obtain very weak support for ergodicity as the test generally rejects the null of ergodicity for most countries excluding Finland, France, Italy, Sweden, and the UK, which may reflect the size distortion shown in Domowitz and El-Gamal (2001).

Table II around here

Next, we report our max half-life (MHL) estimates for the SMM (mixingale) and SMD properties in Tables III and IV, respectively, for the smoothing parameter (*k*) ranging from 1 to 10 to check how robust our estimates are to the choice of bandwidth. We also report max quarter-life (MQL) estimates for SMM and SMD in Tables V and VI, respectively. In addition, we provide graphical representations of our estimates for these properties by plotting all normalized *MDM*(*s*) and $\phi(s)$ for *k* from 1 to 10 in Figures 1 and 2, for SMM and SMD, respectively.

As we can see in Figure 1, normalized MDM(s) decline rapidly for all k with exceptions of Canada and Japan, which imply strong evidence of SMM. Similarly, $\phi(s)$ decrease rapidly with exceptions of those two countries for all k which implies evidence in favor of SMD. Note that MHL for SMM are converging each other as k increases toward 10 where the MHL for k = 10 becomes an upper limit for most countries, while the MHL is not well-defined for Canada and Japan even when k = 10. Similarly, the MHL is not well-defined for these two countries when we investigate persistence based on the SMD property, while we obtain well-defined MHLs for the rest.

Estimated MHLs for SMM range from 0.888 to 4.141 when we use the rule of thumb k, while obtain much longer values when k = 10, even though most MHLs

converge as the smoothing parameter increases to k = 10. MHL estimates for SMD range from 0.940 to 4.985 when k = 1, which are longer than those for SMM. Again, with exceptions of Japan and Canada, convergence was made for most countries, implying that MHLs when k = 10 serve as an upper-limit. Naturally, MQL estimates for SMM and SMD are longer than estimated MHLs, but resemble similar movements as those of MHLs. Convergence were not made only for Canada and Japan.

These findings suggest strong support for a century of PPP in the sense that we find reasonably fast convergence rate toward the long-run equilibrium in a general nonlinear framework.

Tables III, IV, V, and VI around here Figures 1 and 2 around here

In addition, this paper also investigates possible non-monotonic adjustments toward the long-run equilibrium by a metric developed by Steinsson (2008) for linear models. Note that MHL should equal to MQL – MHL if the adjustment takes place monotonically. As we can see in Tables VII and VIII for SMM and SMD, respectively, mostly negative values were obtained especially when *k* is small. This implies the speed of adjustment is faster in the first half compared with that during the second half.⁴

Tables VII and VIII around here

IV Concluding Remarks

⁴ Steinsson (2008) reports mostly positive estimates using the US real exchange rate data for the post-Bretton Woods system, which may be consistent with hump-shape dynamics.

We estimate the persistence of 16 over hundred-year long real exchange rate relative to the US dollar by a nonlinear nonparametric approach suggested by El-Gamal and Ryu (2006). We first obtain conditional and unconditional kernel density functions to obtain nonparametric measures of the speed of convergence towards the long-run equilibrium. That is, we study not only the convergence in the first moment (SMM) but also in distribution (SMD).

Our nonprametric estimates for the persistence are substantially shorter compared with those from linear models, which is consistent with Taylor (2001). Our estimates seem robust to the choice of the smoothing parameter with exceptions of Canada and Japan. The results are consistent with other research such as Kim and Moh (2010) who report strong evidence in favor of PPP by nonparametric AR models for most long-horizon real exchange rates but Canada and Japan.

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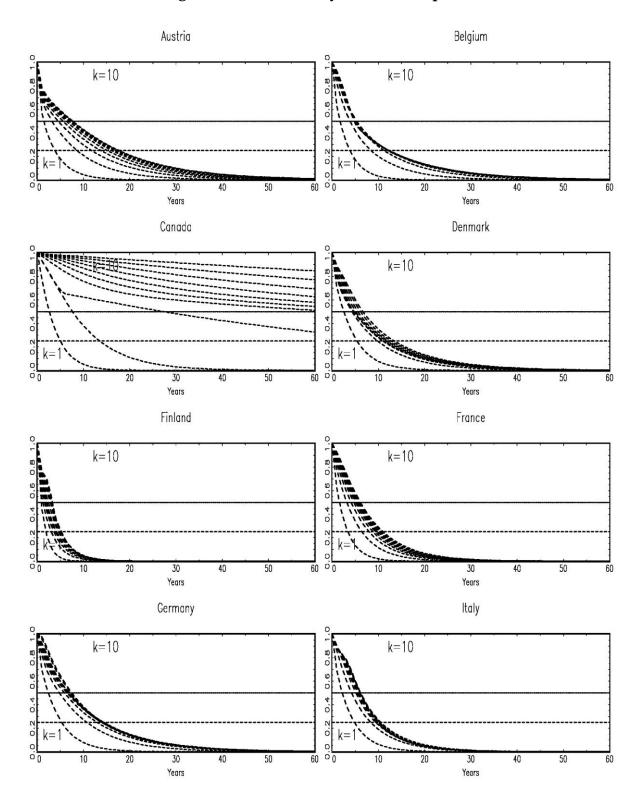
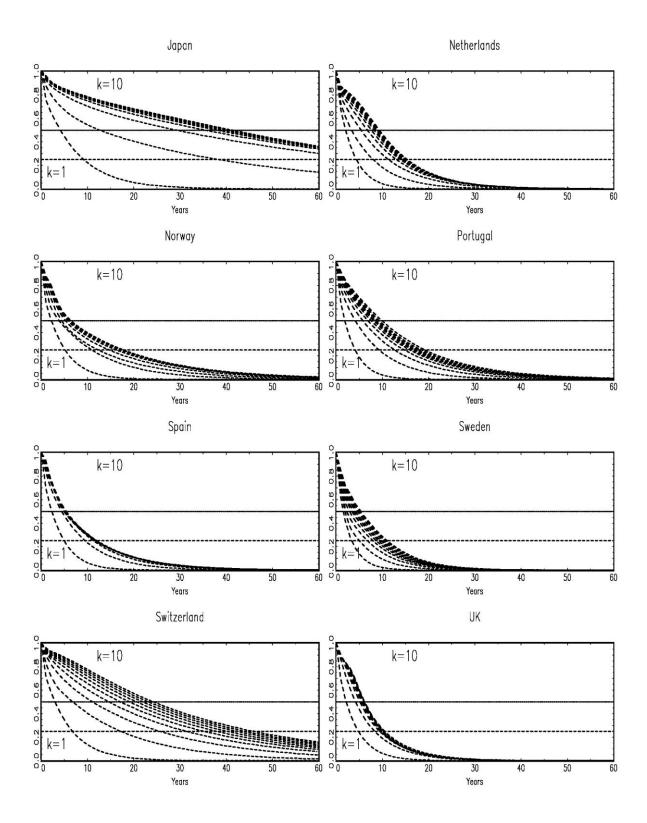


Figure 1. Short-Memory in Mean Properties



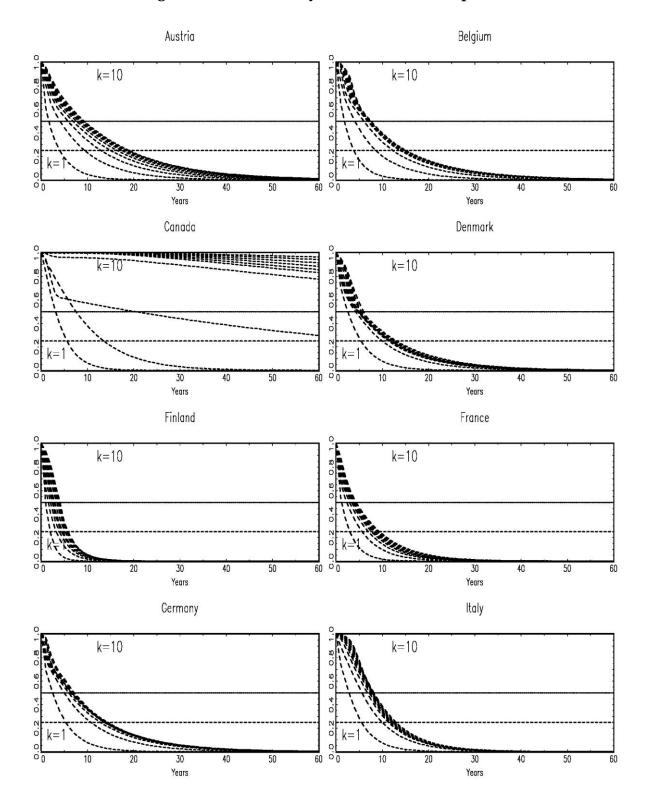
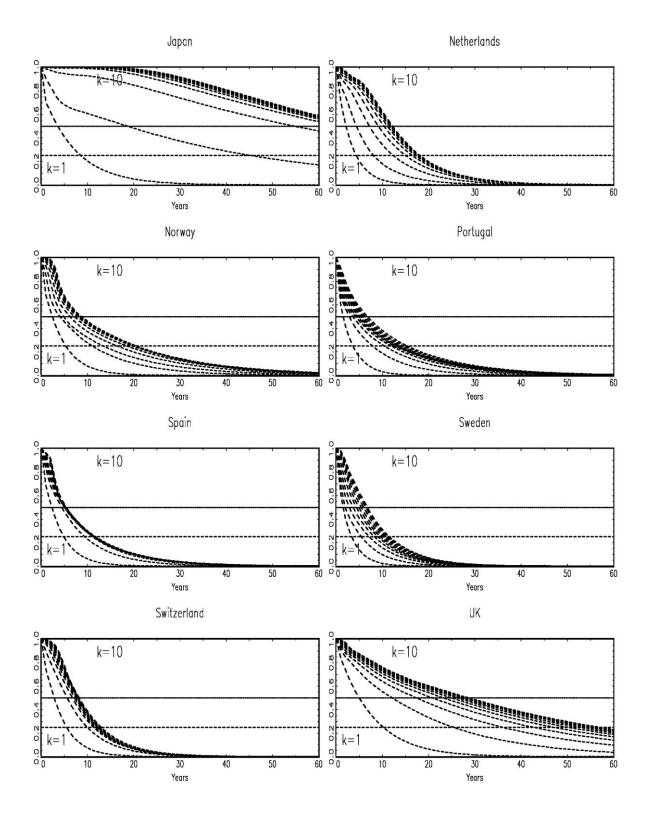


Figure 2. Short-Memory in Distribution Properties



Country	Sample Period	HL	LB	UB
Austria	1870 - 2004	9.746	4.295	8
Belgium	1880 - 1998	3.983	2.186	12.644
Canada	1870 - 2004	10.832	4.613	∞
Denmark	1880 - 2004	8.484	3.824	∞
Finland	1881 - 1998	2.049	1.282	4.298
France	1880 - 1998	5.911	3.188	105.3
Germany	1880 - 1998	16.924	5.674	∞
Italy	1880 - 1998	3.832	1.984	9.903
Japan	1885 - 2004	∞	19.204	8
Netherlands	1870 - 1998	12.035	4.956	∞
Norway	1870 - 2004	8.047	3.986	∞
Portugal	1890 - 1998	5.774	2.867	55.836
Spain	1880 - 1998	7.597	3.784	∞
Sweden	1880 - 2004	4.983	2.654	37.398
Switzerland	1880 - 2004	∞	9.757	∞
UK	1870 - 2004	4.981	2.714	38.162

Table I. Half-Life Estimation from a Linear Model

Note: i) All real exchange rates are relative to the US dollar. ii) The point estimate and the 95% confidence interval are corrected for median bias by Hansen's (1999) grid bootstrap method. For this, 500 bootstrap simulations on each of 30 fine grid points plus minus 6 times the LS standard error around the LS point estimate were implemented. iii) The number of lags was chosen by the general-to-specific rule with a maximum 6 lags.

	Ergodicity		Mixing	
Country	$\Pr(pv < 0.05)$	$\Pr(pv < 0.10)$	$\Pr(pv < 0.05)$	$\Pr(pv < 0.10)$
Austria	13	20	3	9
Belgium	13	21	3	7
Canada	16	25	5	10
Denmark	15	24	4	8
Finland	4	8	3	8
France	6	12	3	7
Germany	13	21	4	8
Italy	5	10	4	7
Japan	40	48	35	42
Netherlands	9	18	3	8
Norway	23	32	69	1
Portugal	9	17	4	9
Spain	11	19	5	11
Sweden	6	11	4	8
Switzerland	17	26	5	11
UK	6	14	4	8

Table II. Tests for Ergodicity and Mixing

Note: i) All real exchange rates are relative to the US dollar. ii) These are randomized tests proposed by Domowitz and El-Gamal (2001). iii) The numbers in the table are the percentage of rejections at the 5% and the 10% significance level, respectively, from 1,000 independent randomized runs.

Country	k = 1	k = 10	Convergence
Austria	1.429	7.656	Yes
Belgium	1.713	4.765	Yes
Canada	2.611	<i>n.a.</i>	No
Denmark	2.525	6.673	Yes
Finland	0.888	3.287	Yes
France	1.596	6.094	Yes
Germany	2.381	7.491	Yes
Italy	2.167	6.118	Yes
Japan	4.141	41.375	Yes
Netherlands	2.023	9.353	Yes
Norway	2.179	6.400	Yes
Portugal	1.872	9.919	Yes
Spain	2.275	5.043	Yes
Sweden	1.561	5.362	Yes
Switzerland	2.958	24.313	Yes
UK	2.167	6.118	Yes

Table III. Maximum Half Life Estimation: SMM

Country	k = 1	k = 10	Convergence
Austria	1.625	9.296	Yes
Belgium	1.798	7.545	Yes
Canada	3.087	<i>n.a.</i>	No
Denmark	2.509	5.875	Yes
Finland	0.940	4.034	Yes
France	1.177	4.321	Yes
Germany	2.466	7.176	Yes
Italy	2.797	8.155	Yes
Japan	3.581	<i>n.a.</i>	No
Netherlands	2.123	12.227	Yes
Norway	2.402	8.731	Yes
Portugal	1.521	6.810	Yes
Spain	2.283	5.392	Yes
Sweden	1.529	6.724	Yes
Switzerland	2.797	8.155	Yes
UK	4.985	28.732	Yes

Table IV. Maximum Half Life Estimation: SMD

Country	k = 1	k = 10	Convergence
Austria	3.803	17.667	Yes
Belgium	3.833	12.350	Yes
Canada	4.942	<i>n.a.</i>	No
Denmark	5.383	13.458	Yes
Finland	1.882	5.169	Yes
France	3.407	11.000	Yes
Germany	5.259	14.080	Yes
Italy	4.803	10.538	Yes
Japan	9.182	<i>n.a.</i>	No
Netherlands	4.384	15.367	Yes
Norway	5.145	17.625	Yes
Portugal	4.086	19.263	Yes
Spain	4.920	11.929	Yes
Sweden	3.391	11.094	Yes
Switzerland	6.755	45.875	Yes
UK	4.803	10.538	Yes

Table V. Maximum Quarter Life Estimation: SMM

Country	k = 1	k = 10	Convergence
Austria	3.984	18.966	Yes
Belgium	3.827	15.157	Yes
Canada	5.544	n.a.	No
Denmark	5.382	13.077	Yes
Finland	1.923	5.785	Yes
France	2.950	9.437	Yes
Germany	5.292	14.339	Yes
Italy	5.480	12.948	Yes
Japan	8.563	<i>n.a.</i>	No
Netherlands	4.336	18.154	Yes
Norway	5.303	20.366	Yes
Portugal	3.624	15.424	Yes
Spain	4.868	11.570	Yes
Sweden	3.364	11.555	Yes
Switzerland	5.480	12.948	Yes
UK	10.214	56.870	Yes

Table VI. Maximum Quarter Life Estimation: SMD

Country	k = 1	k = 10	Convergence
Austria	-0.945	-2.355	Yes
Belgium	-0.407	-2.820	Yes
Canada	0.280	<i>n.a.</i>	No
Denmark	-0.333	-0.112	Yes
Finland	-0.106	1.405	Yes
France	-0.215	1.188	Yes
Germany	-0.497	0.902	Yes
Italy	-0.469	1.698	Yes
Japan	-0.900	3.917	No
Netherlands	-0.338	3.339	Yes
Norway	-0.787	-4.825	Yes
Portugal	-0.342	0.575	Yes
Spain	-0.370	-1.843	Yes
Sweden	-0.269	-0.370	Yes
Switzerland	-0.830	2.751	Yes
UK	-0.469	1.698	Yes

Table VII. Monotonic Convergence (2MHL – MQL): SMM

Note: i) All real exchange rates are relative to the US dollar. ii) Estimates are calculated by linear interpolations. iii) 2MHL - MQL is adopted from Steinsson (2008). Zero values for 2MHL - MQL imply monotonic adjustment process towards the long-run equilibrium. Negative values occur when MHL < MQL - MHL.

Country	k = 1	k = 10	Convergence
Austria	-0.734	-0.374	Yes
Belgium	-0.231	-0.067	Yes
Canada	0.630	<i>n.a.</i>	No
Denmark	-0.364	-1.327	Yes
Finland	-0.043	2.283	Yes
France	-0.596	-0.795	Yes
Germany	-0.360	0.013	Yes
Italy	0.114	3.362	Yes
Japan	-1.401	<i>n.a.</i>	No
Netherlands	-0.090	6.300	Yes
Norway	-0.499	-2.904	Yes
Portugal	-0.582	-1.804	Yes
Spain	-0.302	-0.786	Yes
Sweden	-0.306	1.893	Yes
Switzerland	0.114	3.362	Yes
UK	-0.244	0.594	Yes

Table VIII. Monotonic Convergence: SMD

Note: i) All real exchange rates are relative to the US dollar. ii) Estimates are calculated by linear interpolations. iii) 2MHL - MQL is adopted from Steinsson (2008). Zero values for 2MHL - MQL imply monotonic adjustment process towards the long-run equilibrium. Negative values occur when MHL < MQL - MHL.